

# Métodos de Caracterización Dieléctrica



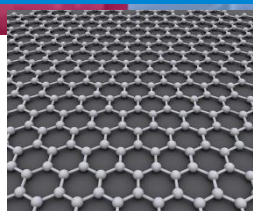
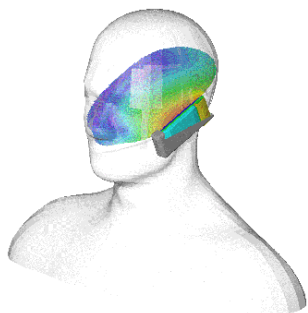
**Adolfo Del Solar**

Application Engineer  
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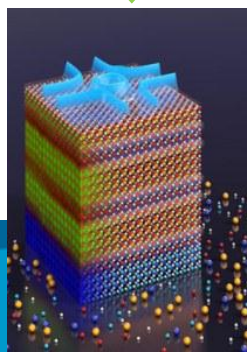
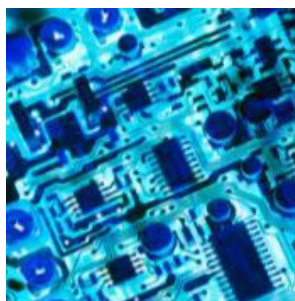
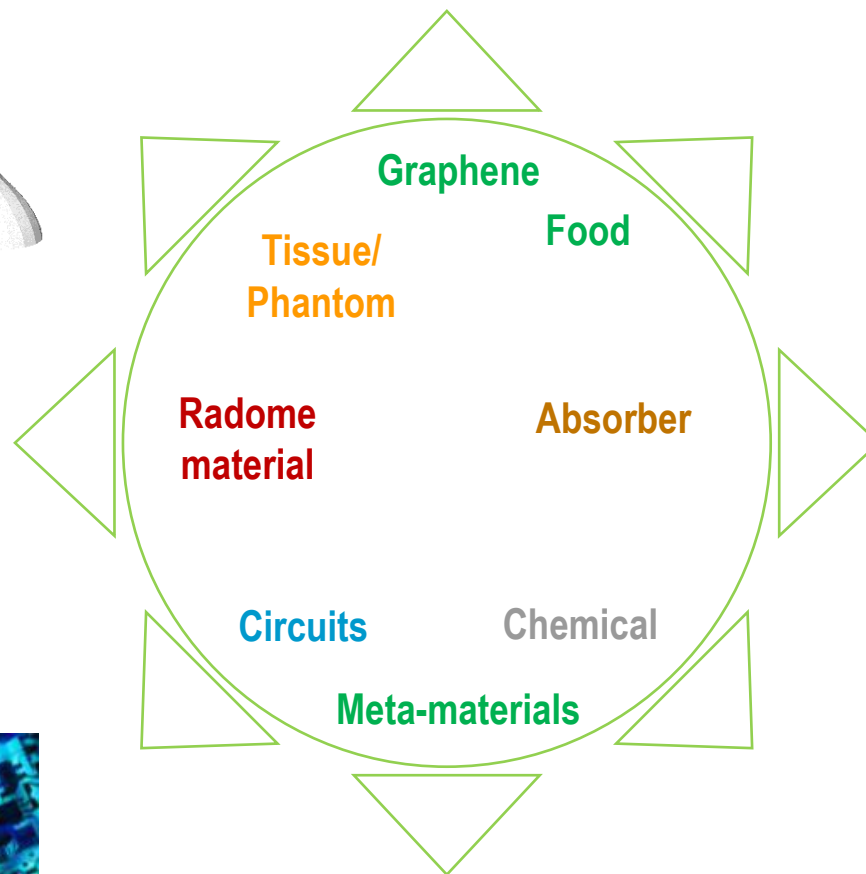
- **Introduction**
- **Permittivity and permeability**
- **Measurement techniques and systems**
- **Parallel plate**
- **Coaxial probe**
- **Transmission line**
- **Free space**
- **Resonant cavity**

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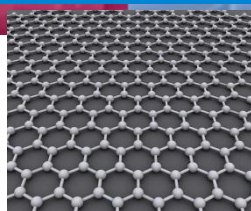
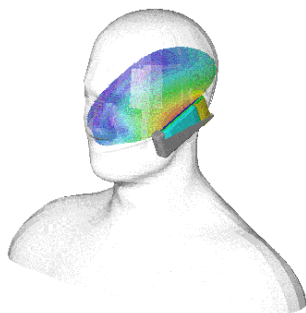
# Type of material



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**TECHNOLOGIES**  
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# Type of material

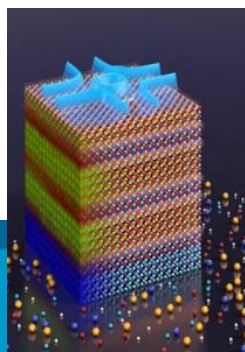
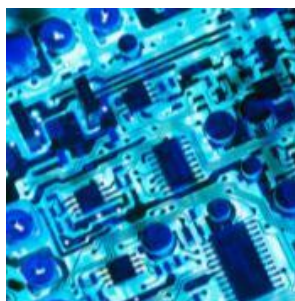


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Industry	Application/Products
Electronics	Capacitors, substrates, PCB antennas, ferrites, absorbers, SAR phantom materials
Aerospace/Defense	Stealth, RAM (radiation absorbing materials), radomes
Industrial/Materials	Ceramics & composites: A/D and automotive components, coatings Polymers & plastics: Fibers, films, Insulation materials Hydrogel: Disposable diaper, soft contact lens Liquid crystal: Displays Other products containing these materials: Tires, paint, adhesives, etc.
Food & Agriculture	Food preservation (spoilage) research, food development for microwave, packaging, moisture measurements
Mining	Moisture measurements in wood or paper, oil content analysis
Pharmaceutical & Medical	Drug research and manufacturing, bio-implants, human tissue characterization, biomass, fermentation



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## Permittivity (Dielectric Constant)

$$K = \frac{\epsilon}{\epsilon_0} = \epsilon_r = \epsilon_r' - j\epsilon_r''$$

interaction of a material in the presence  
of an external electric field.



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interaction of a material in the presence of an external electric field.

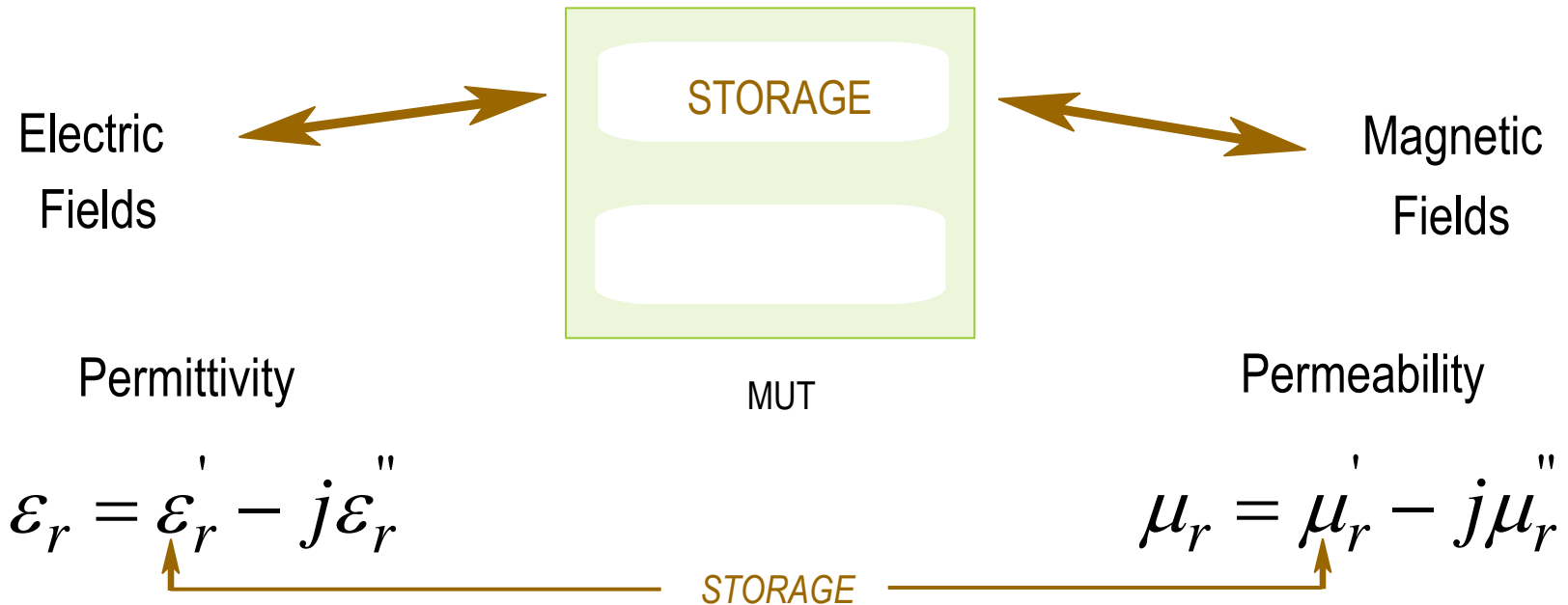
## Permeability

$$\mu = \frac{\mu}{\mu_0} = \mu_r' - j\mu_r''$$

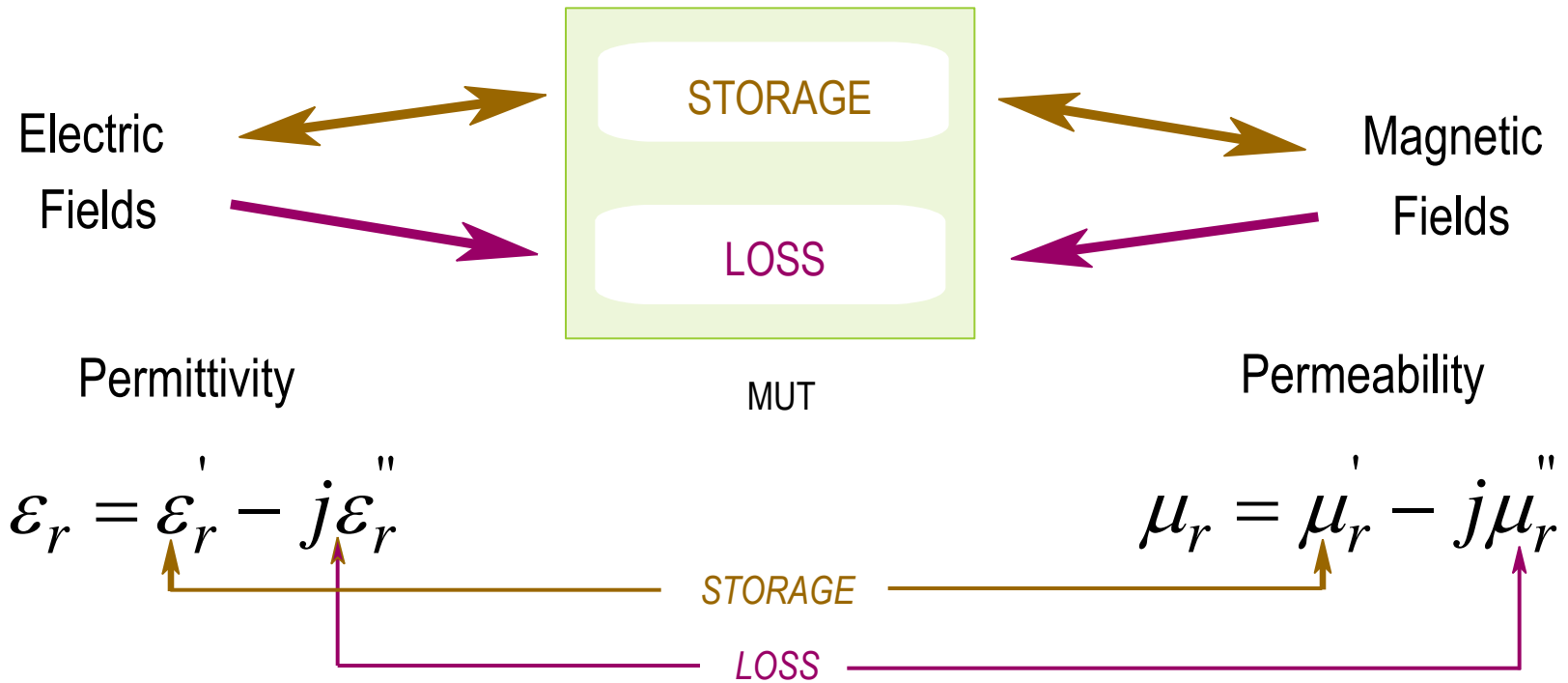
interaction of a material in the presence of an external magnetic field.



# Electromagnetic field interaction

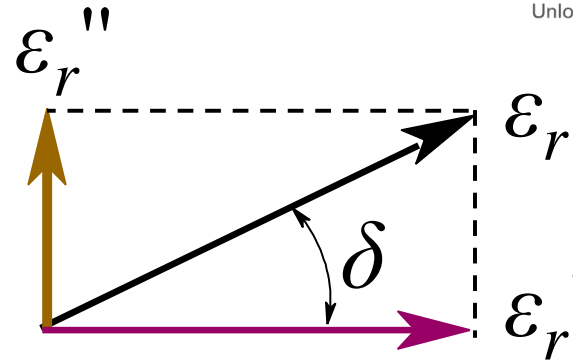


# Electromagnetic field interaction



# Loss tangent

$$\tan \delta = \frac{\epsilon_r''}{\epsilon_r'}$$



$$\tan \delta = D = \frac{1}{Q} = \frac{\text{Energy Lost per Cycle}}{\text{Energy Stored per Cycle}}$$

**D**

Dissipation Factor

**Q**

Quality Factor

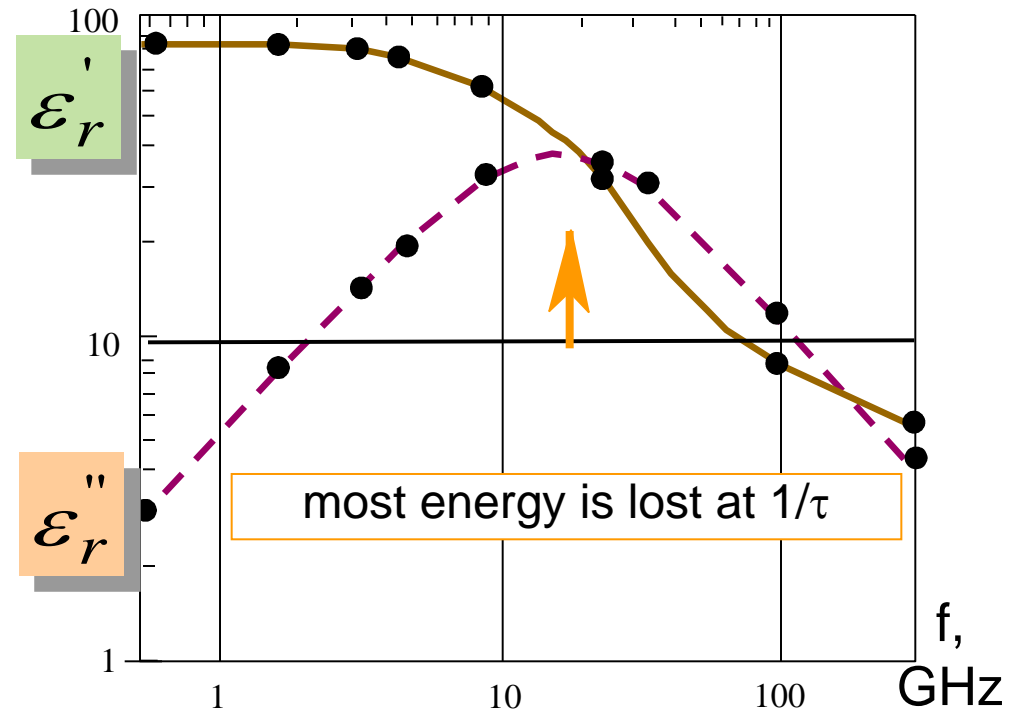
**Df**



# Relaxation constant

$\tau$  = Time required for 1/e of an aligned system to return to equilibrium or random state, in seconds.

$$\tau = \frac{1}{\omega_c} = \frac{1}{2\pi f_c}$$



$$\text{Debye equation: } \epsilon(\omega) = \epsilon_\infty + \frac{\epsilon_s - \epsilon_\infty}{1 + j\omega\tau}$$

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# Material evaluation measurement system

Composed by 3 main pieces:

- Precise measurement instruments
- Test fixtures that hold the MUT
- Software that can calculate & display basic material parameters

The measurement instrument and the test fixtures are determined by the **measurement technique** chosen.

# Measurement techniques

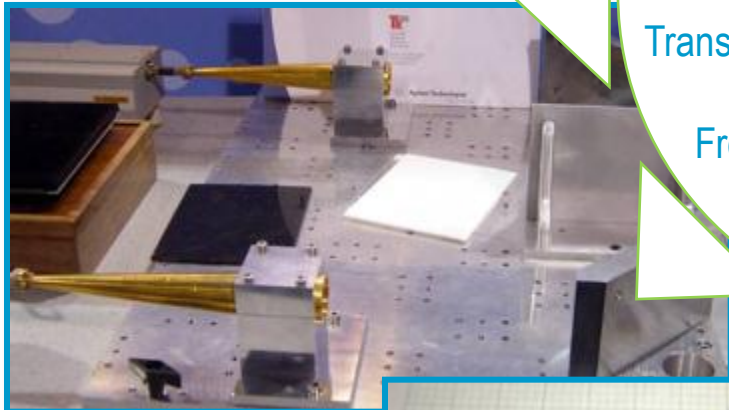


Parallel  
Plate

Coaxial  
Probe

Transmission Line  
&  
Free Space

Resonant  
Cavity





# Which method is best?

It Depends...



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# Which method is best?

## It Depends... on

- ✓ Frequency of interest
- ✓ Expected value of  $\varepsilon_r$  and  $\mu_r$
- ✓ Required measurement accuracy

# Which method is best?

## It Depends... on

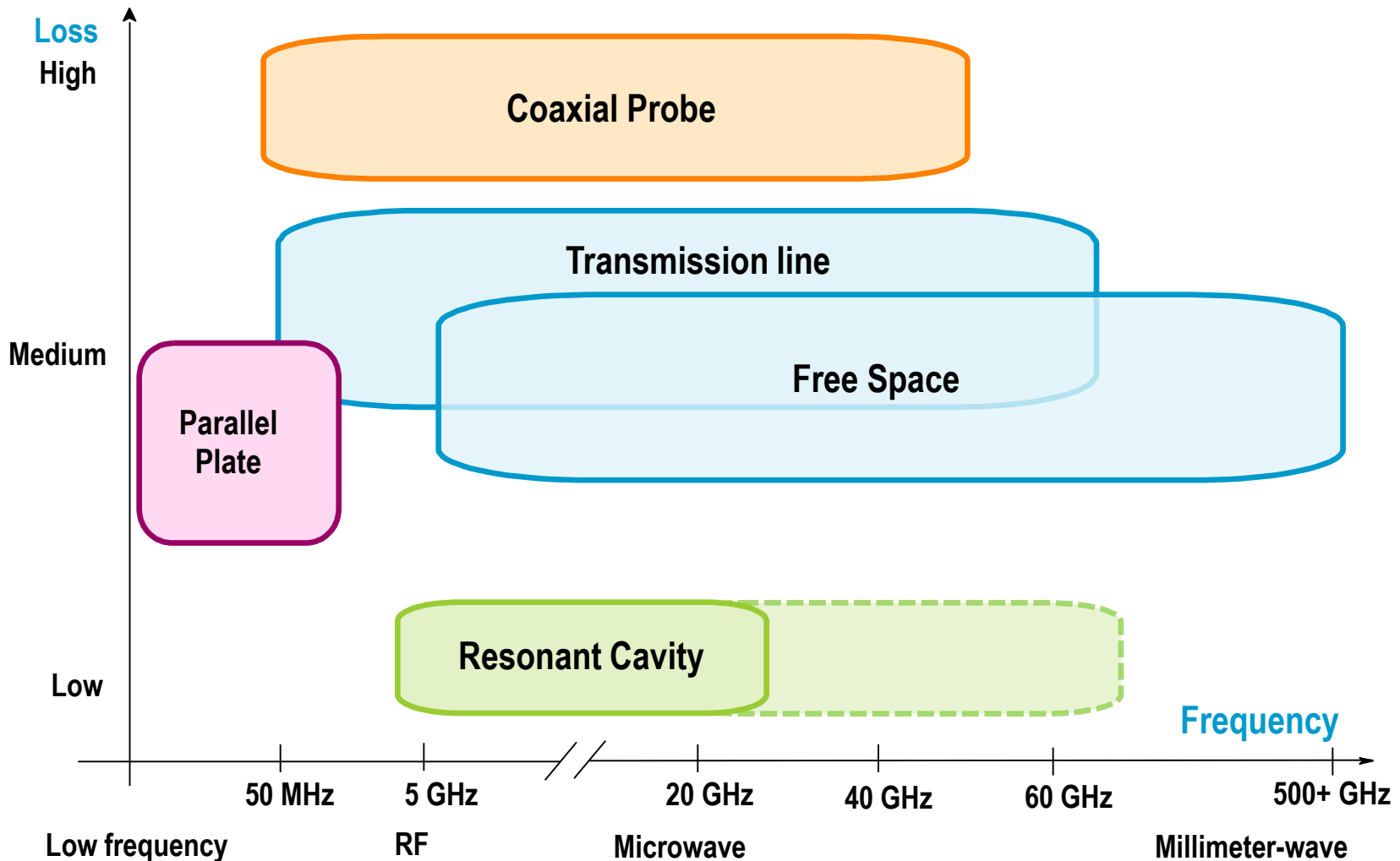
- ✓ Frequency of interest
- ✓ Expected value of  $\epsilon_r$  and  $\mu_r$
- ✓ Required measurement accuracy
- ✓ Material properties (i.e., homogeneous, isotropic)
- ✓ Form of material (i.e., liquid, powder, solid, sheet)
- ✓ Sample size restrictions

# Which method is best?

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- ✓ Frequency of interest
- ✓ Expected value of  $\epsilon_r$  and  $\mu_r$
- ✓ Required measurement accuracy
- ✓ Material properties (i.e., homogeneous, isotropic)
- ✓ Form of material (i.e., liquid, powder, solid, sheet)
- ✓ Sample size restrictions
- ✓ Destructive or non-destructive
- ✓ Contacting or non-contacting
- ✓ Temperature

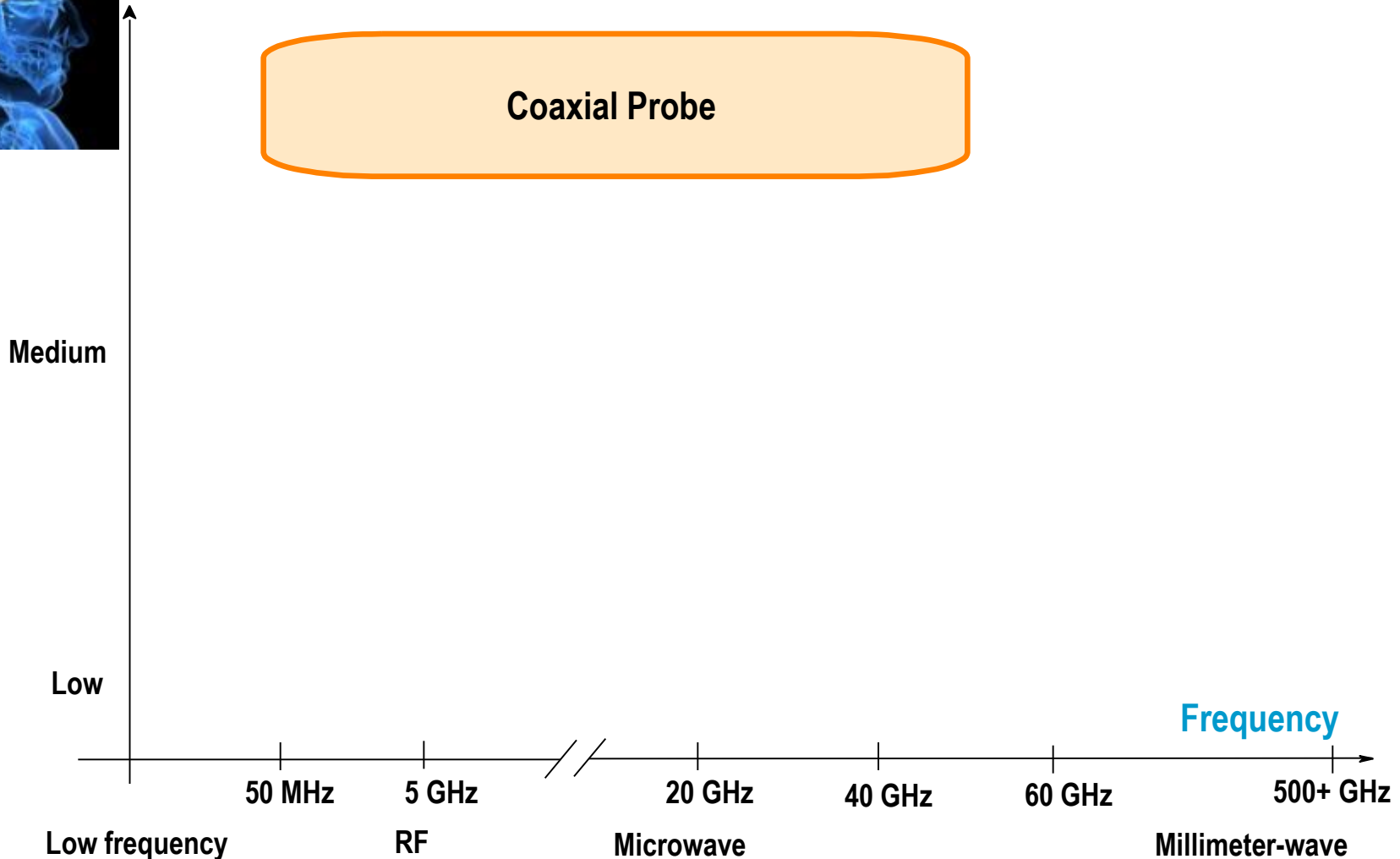
# Measurement methods vs. frequency and material loss



# Measurement methods vs. frequency and material loss



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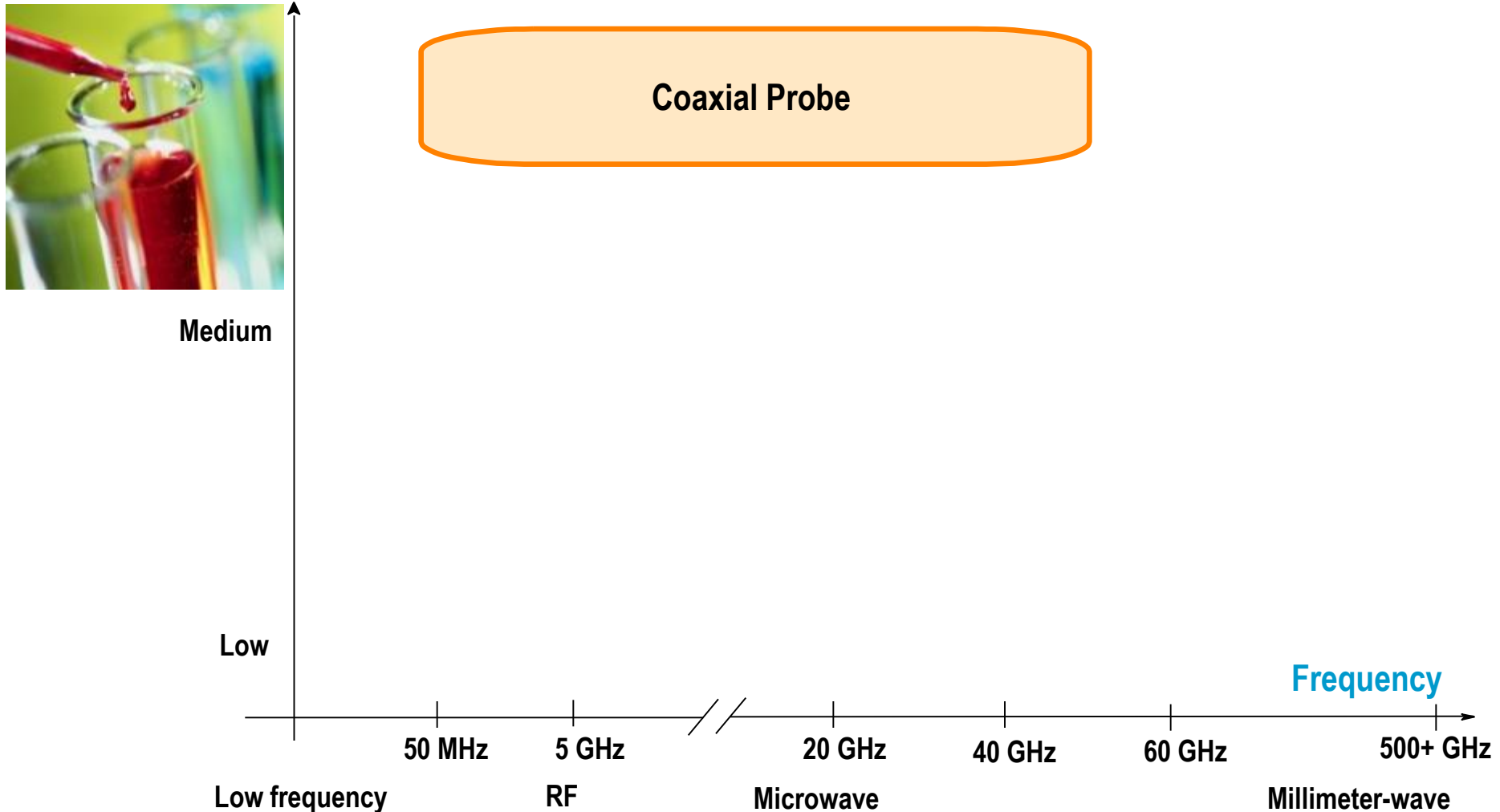
Agilent Technologies

Agilent Technologies  
February 2014

# Measurement methods vs. frequency and material loss

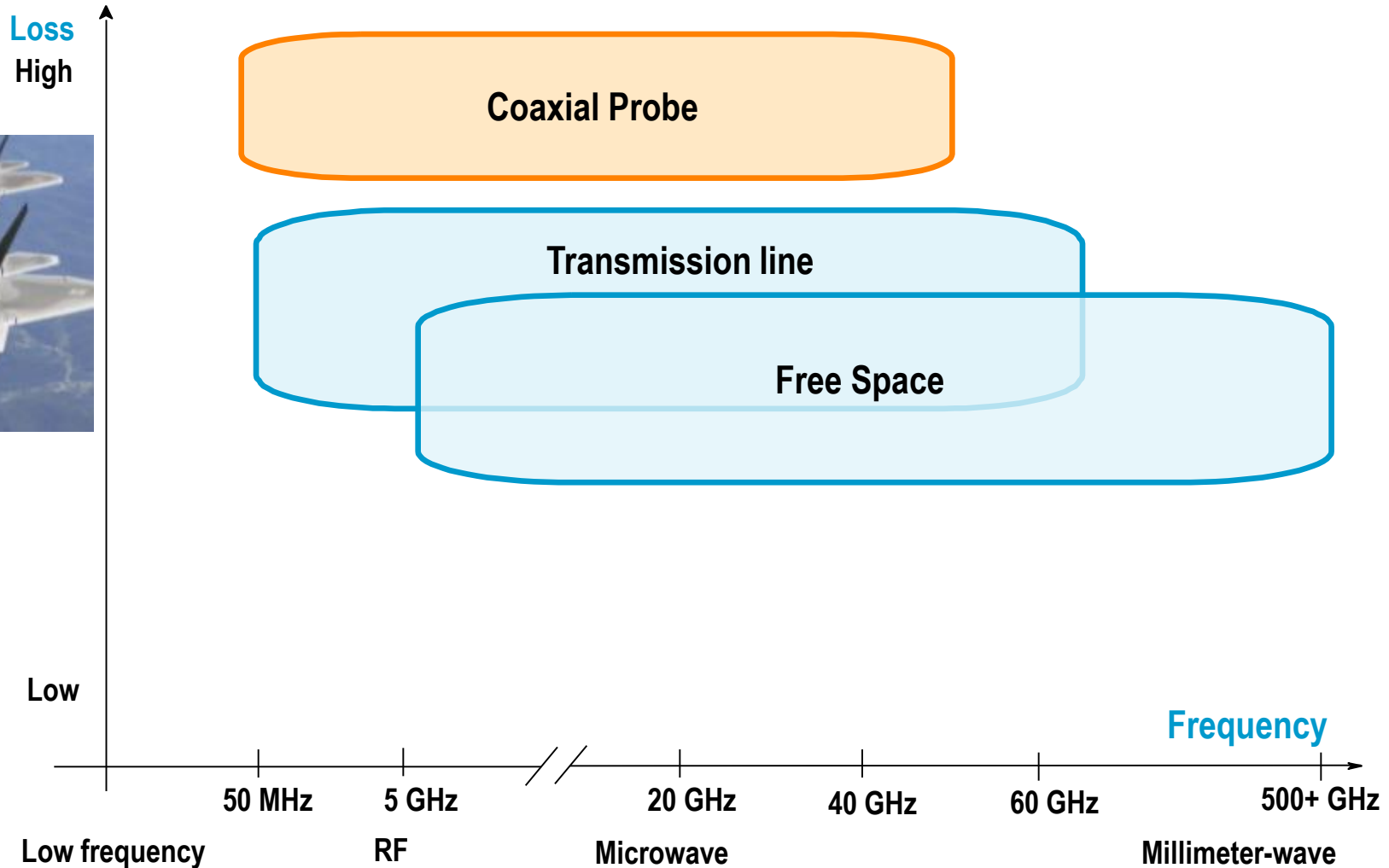


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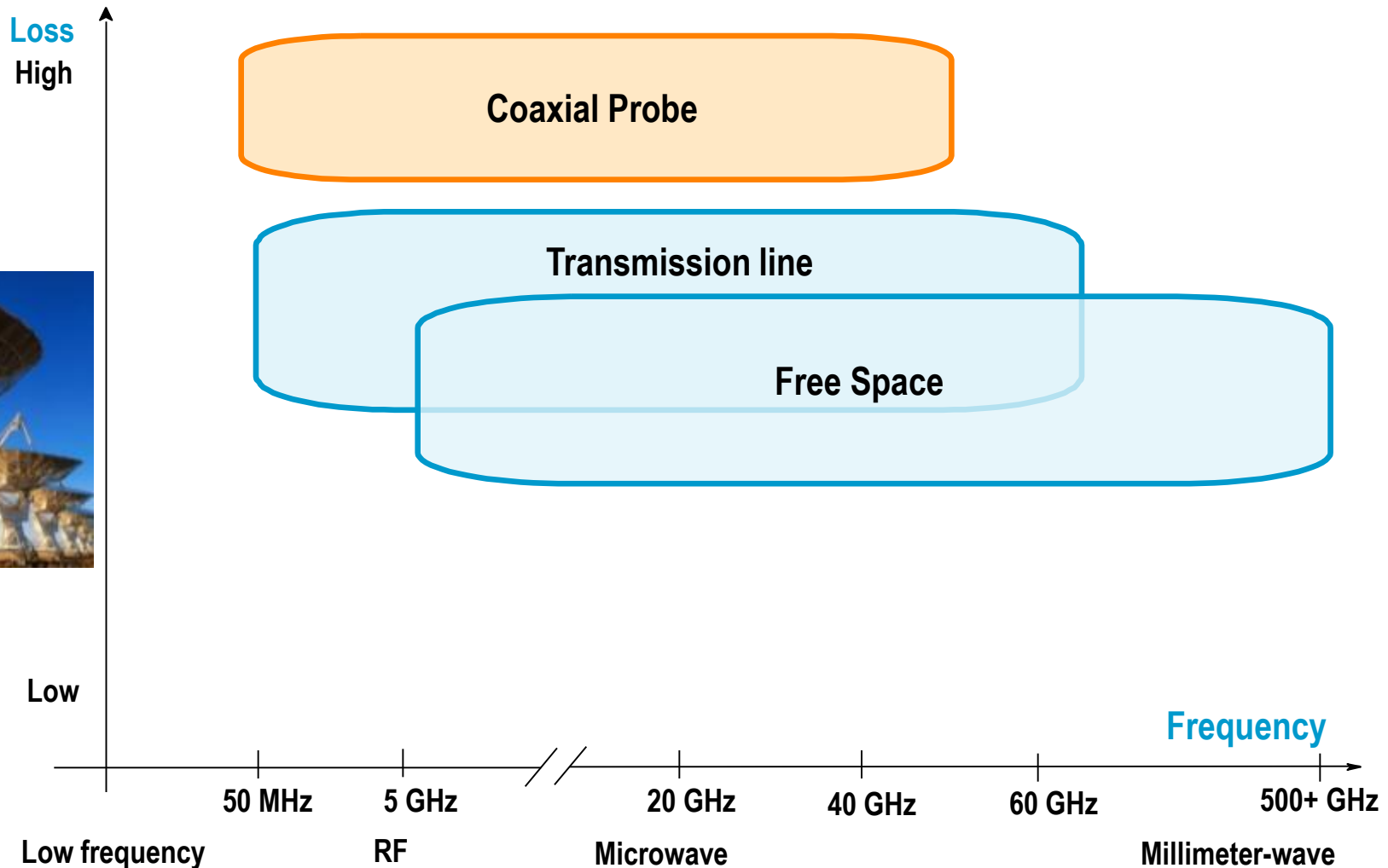




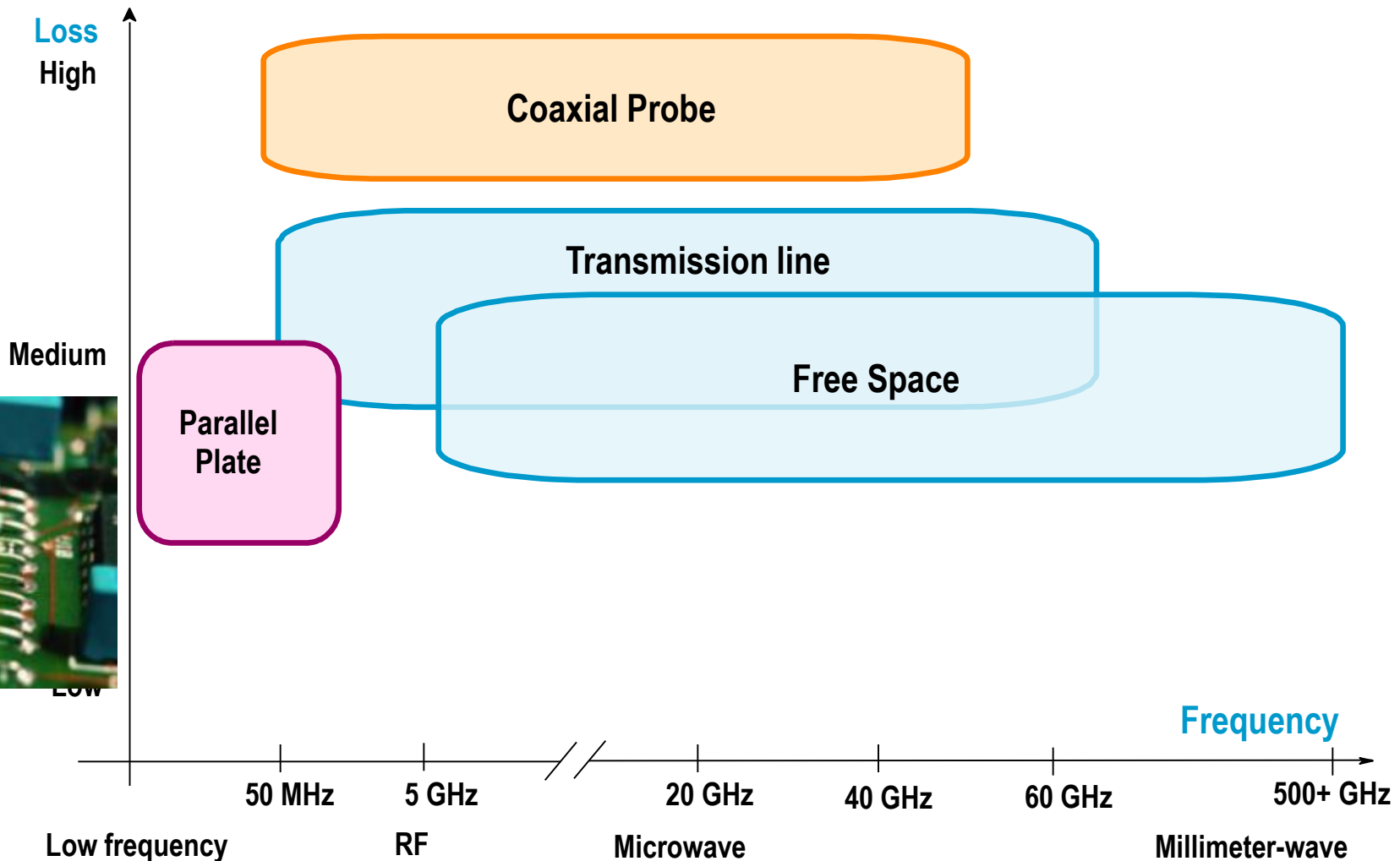
# Measurement methods vs. frequency and material loss



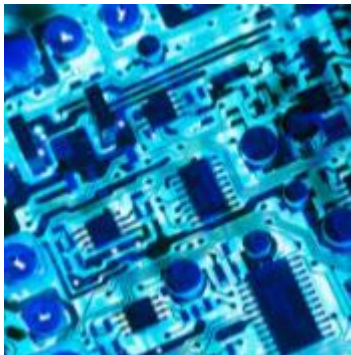
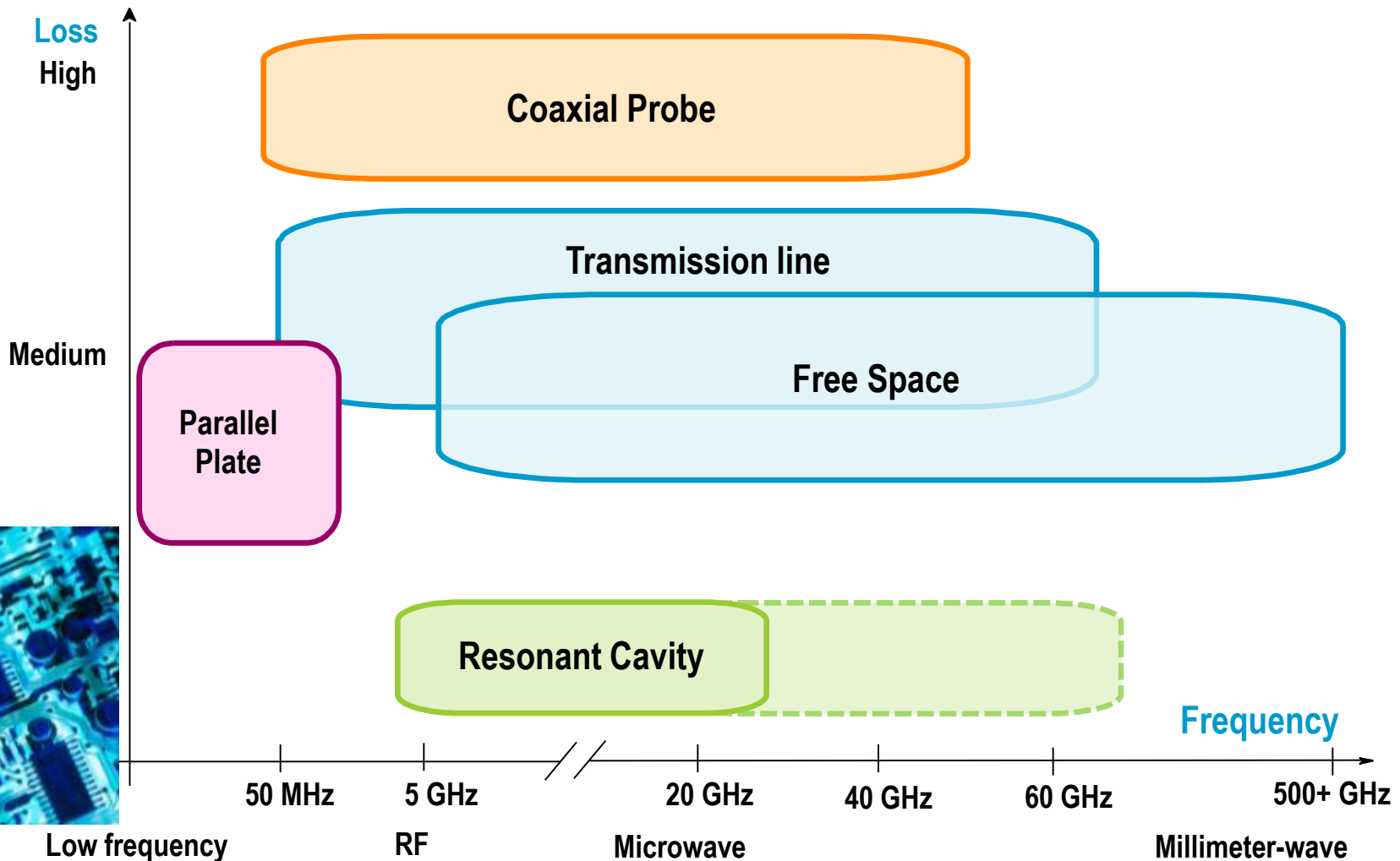
# Measurement methods vs. frequency and material loss



# Measurement methods vs. frequency and material loss



# Measurement methods vs. frequency and material loss



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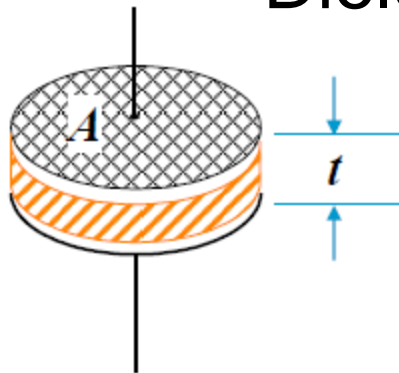
# Parallel plate capacitor system



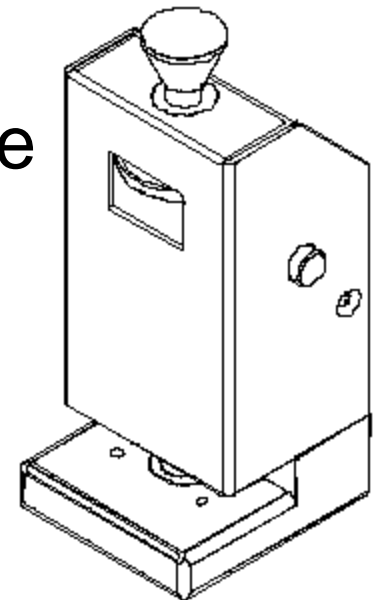
$$\epsilon'_r = \frac{C}{\epsilon_0 \frac{A}{t}}$$

$$\tan \delta = D$$

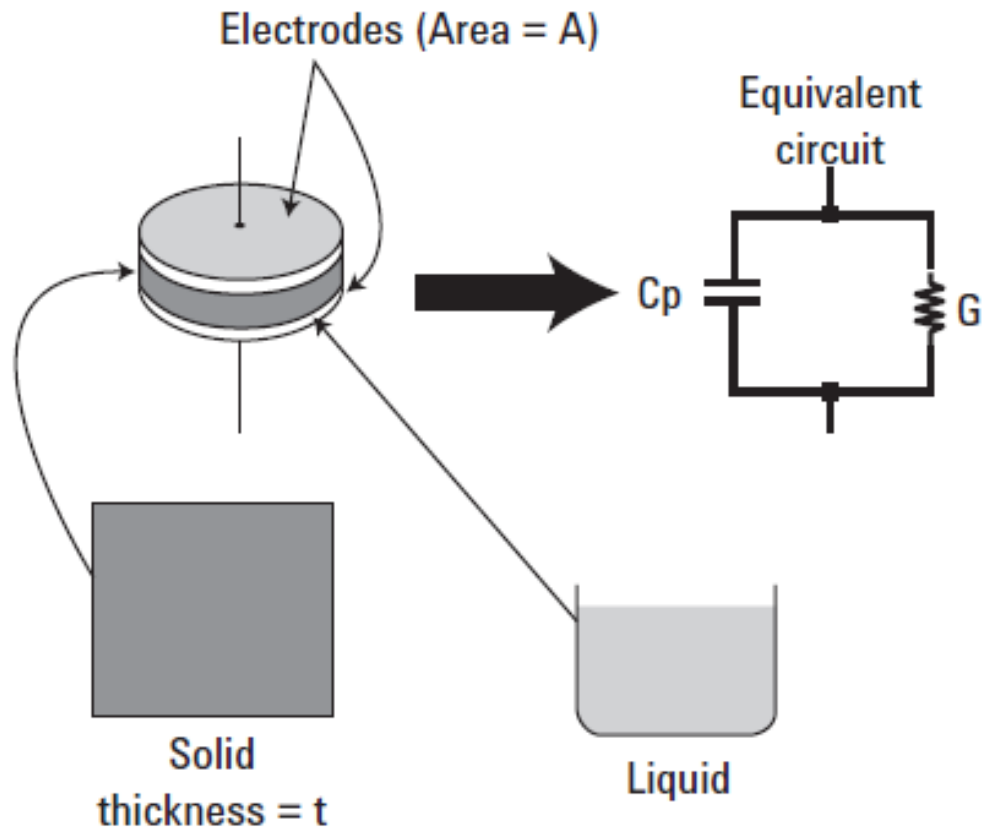
## Dielectric Test Fixture



(magnetic  
fixture also  
available)



# Parallel capacitor technique



$$Y = G + j\omega C_p$$

$$= j\omega C_0 \left( \frac{C_p}{C_0} - j \frac{G}{\omega C_0} \right)$$

C<sub>0</sub> : Air capacitance

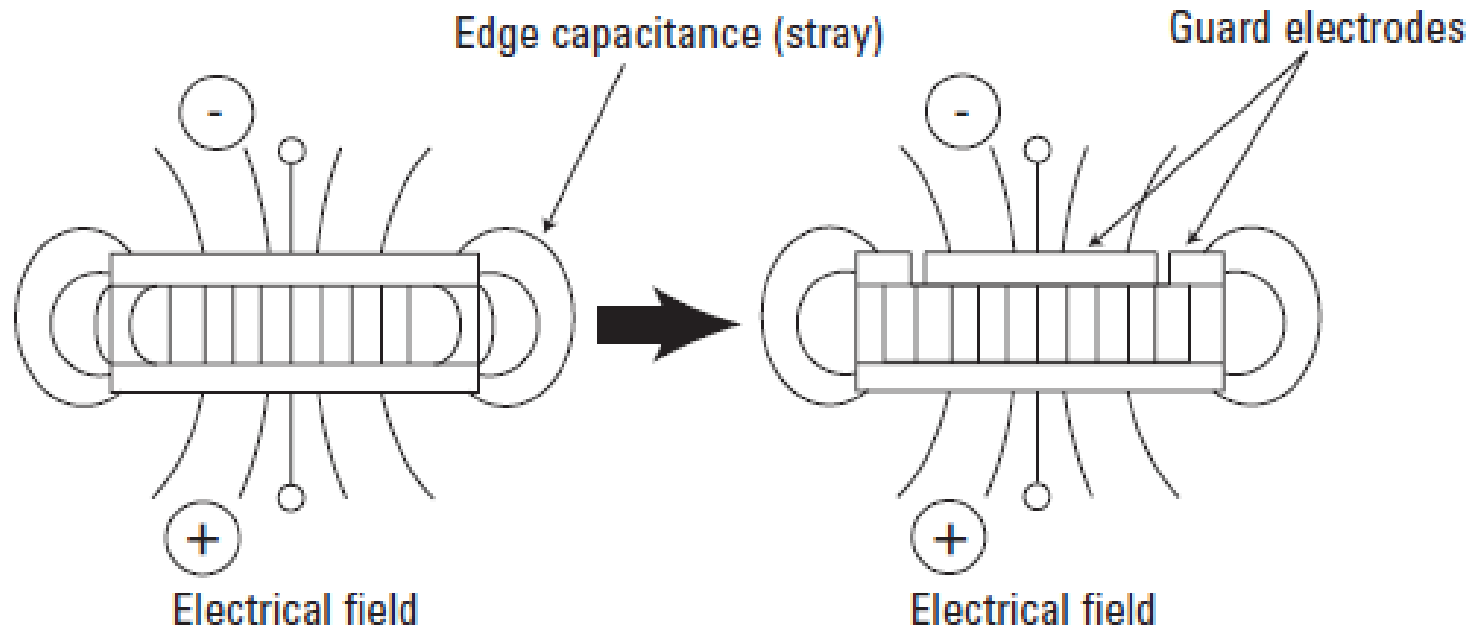
$$\epsilon_r^* = \left( \frac{C_p}{C_0} - j \frac{G}{\omega C_0} \right)$$

$$\epsilon_r' = \left( \frac{t^* C_p}{A^* \epsilon_0} \right)$$

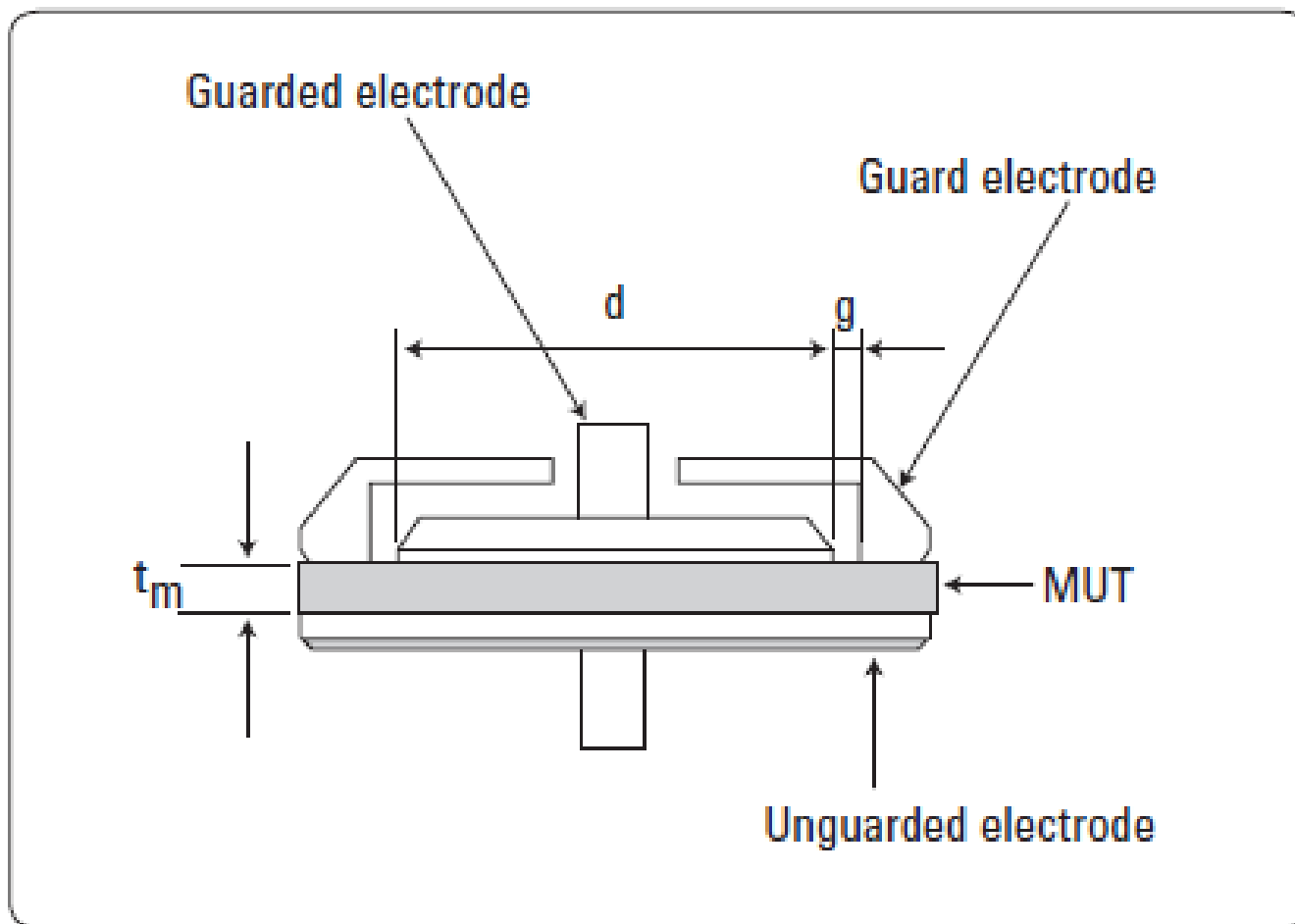
$$\epsilon_r'' = \left( \frac{t}{\omega^* R_p^* A^* \epsilon_0} \right)$$



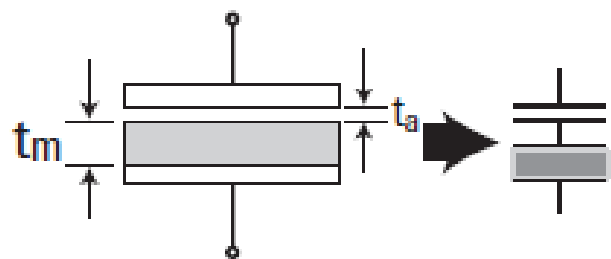
# Effect of guard electrode



# Contacting electrode method



# Air gap effects



$$C_o = \epsilon_o \frac{A}{t_a} \quad \text{Capacitance of airgap}$$

$$C_x = \epsilon_x \epsilon_o \frac{A}{t_m} \quad \text{Capacitance of dielectric material}$$

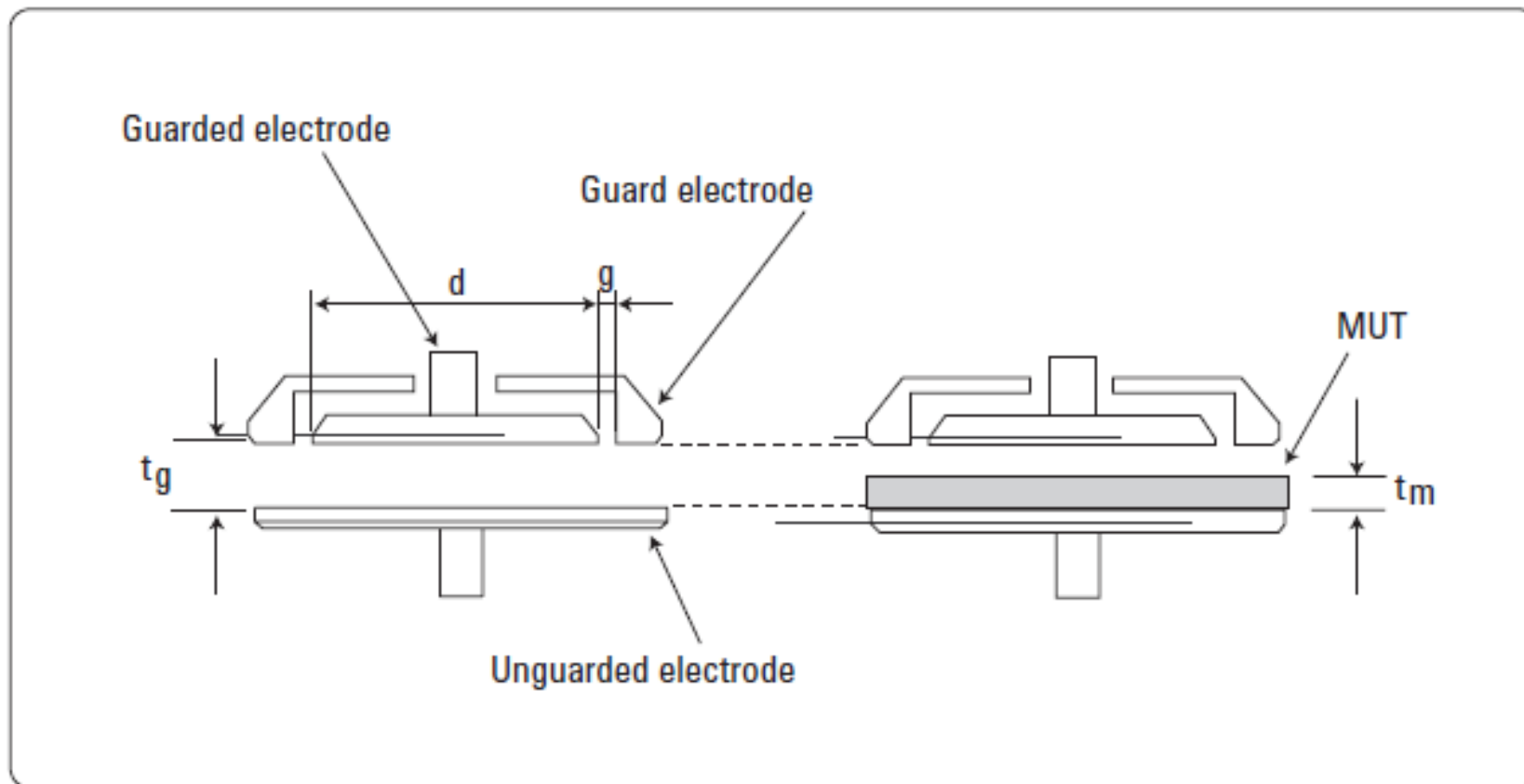
Measured capacitance

$$C_{\text{err}} = \frac{1}{\frac{1}{C_o} + \frac{1}{C_x}} = \epsilon_{\text{err}} \epsilon_o \frac{A}{t_m + t_a}$$

Measured error due to airgap

$$1 - \frac{\epsilon_{\text{err}}}{\epsilon_x} = \frac{\epsilon_x - 1}{\epsilon_x + \frac{t_m}{t_a}}$$

# Non-contacting electrode method



# Parallel plate measurement methods comparison

Method	Accuracy	Application MUT	Operation
Contacting electrode	LOW	Solid material with a flat and smooth surface	1 measurement
Non-Contacting electrode	MEDIUM	Solid material with a flat and smooth surface	2 measurements
Thin film electrode	HIGH	Thin film electrode must be applied onto surfaces	1 measurement

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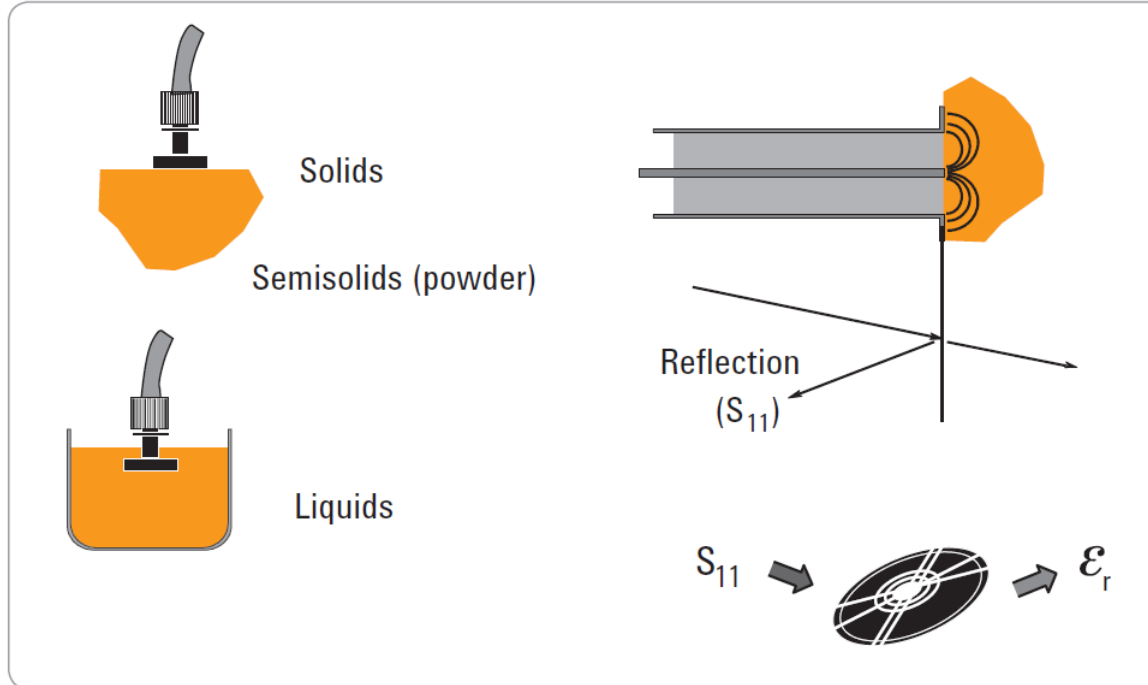
# Coaxial probe system



Dielectric measurement setup for liquid using the coaxial probe method



# Coaxial probe



## Technique features:

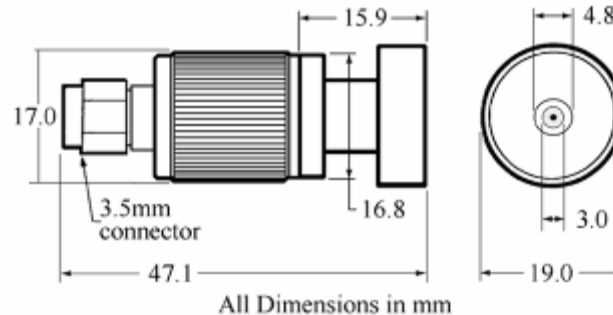
- Broadband
- Simple and convenient (non destructive)
- Limited  $\epsilon_r$  accuracy
- Limited  $\tan \delta$  low loss resolution
- Best for liquids of semi-solids

## Assumptions:

- Semi-infinite thickness
- Non-magnetic material
- Isotropic and homogeneous
- Flat surface
- No air gaps or bubbles

# Three probe designs

## 1. High temperature probe

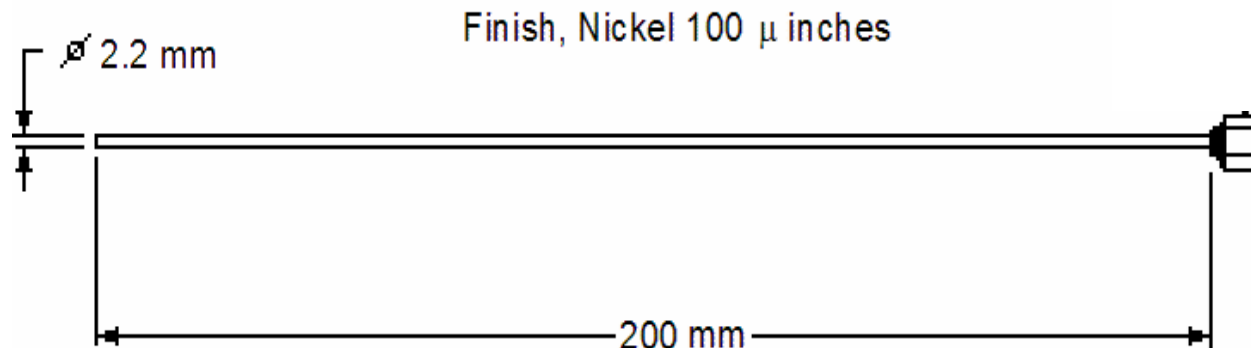


### High Temperature Probe

- 0.200 – 20GHz (low end 0.01GHz with impedance analyzer)
- Withstands -40 to 200 degrees C
- Survives corrosive chemicals
- Flanged design allows measuring flat surfaced solids.

# Three probe designs

## 2. Slim form probe

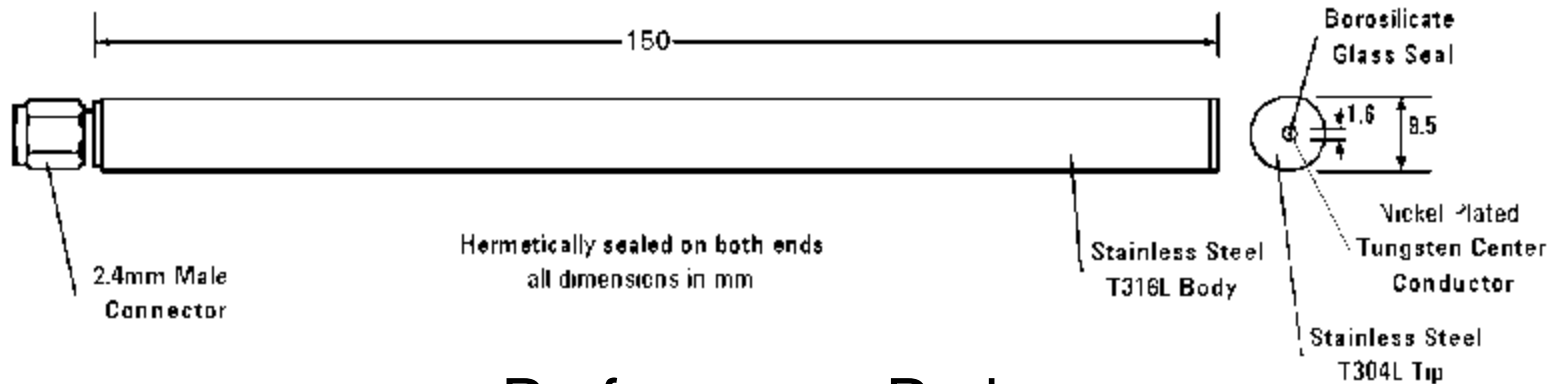


### Slim Form Probe

- 0.500 – 50GHz
- Low cost consumable design
- Fits in tight spaces, smaller sample sizes
- For liquids and soft semi-solids only

# Three probe designs

## 3. Performance probe



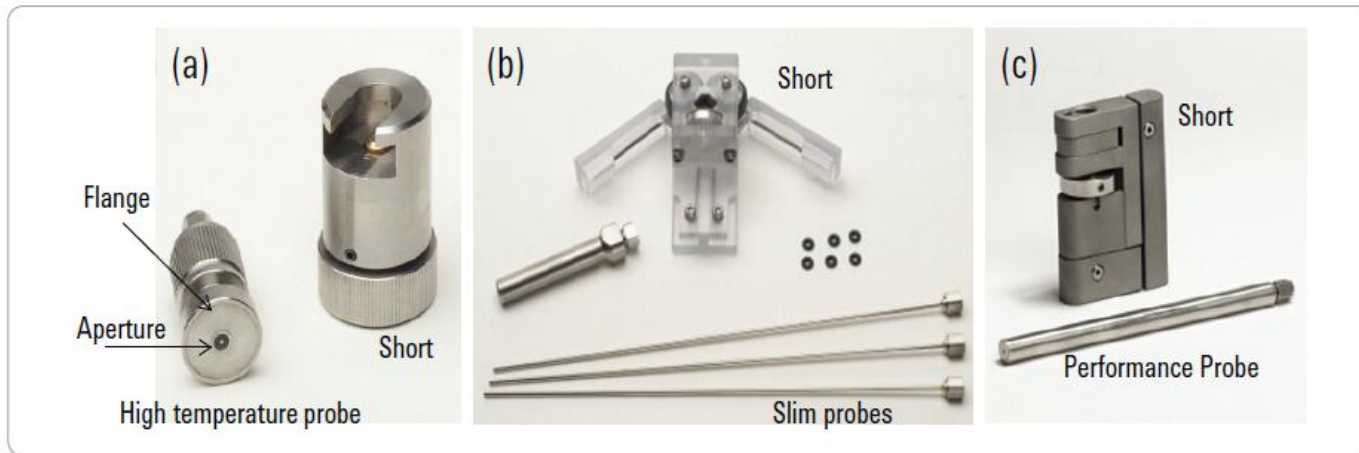
### Performance Probe

Combines rugged high temperature performance with high frequency performance, all in one slim design.

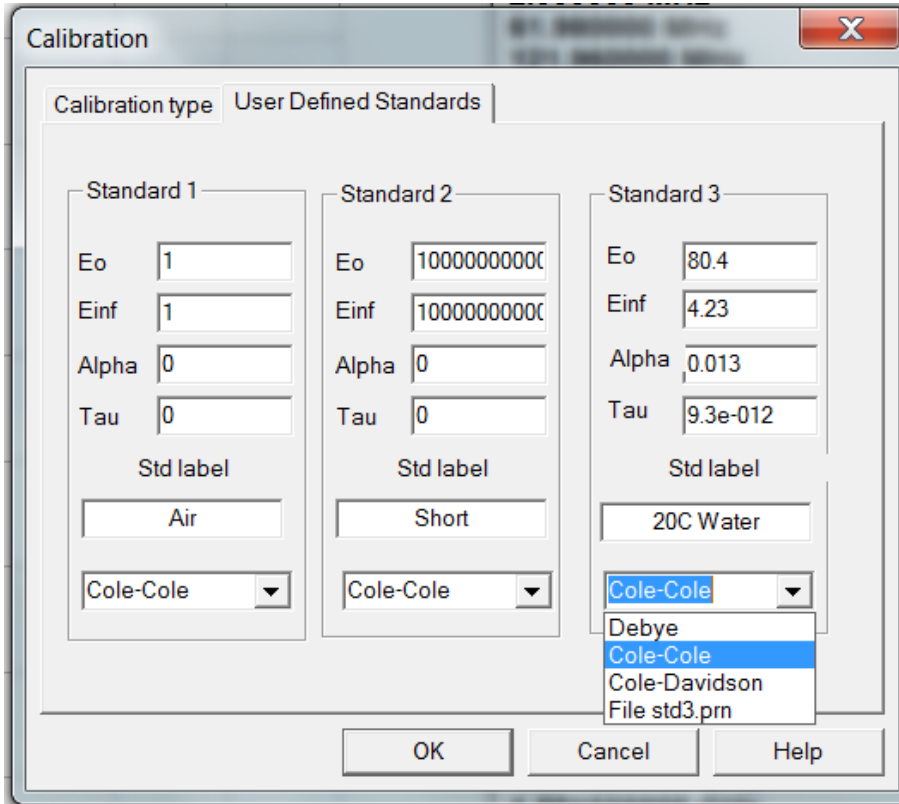
- 0.500 – 50GHz
- Withstands -40 to 200 degrees C
- Hermetically sealed on both ends, OK for autoclave
- Food grade stainless steel

# Coaxial probe system

## Calibration is required!!!



# Coaxial probe system calibration



Calibration

Calibration type: User Defined Standards

Standard 1	Standard 2	Standard 3
Eo: 1	Eo: 10000000000	Eo: 80.4
Einf: 1	Einf: 10000000000	Einf: 4.23
Alpha: 0	Alpha: 0	Alpha: 0.013
Tau: 0	Tau: 0	Tau: 9.3e-012
Std label: Air	Std label: Short	Std label: 20C Water
Cole-Cole	Cole-Cole	Cole-Cole

OK Cancel Help

Three standards:  
Air, Short, Water

Air, Short, Load

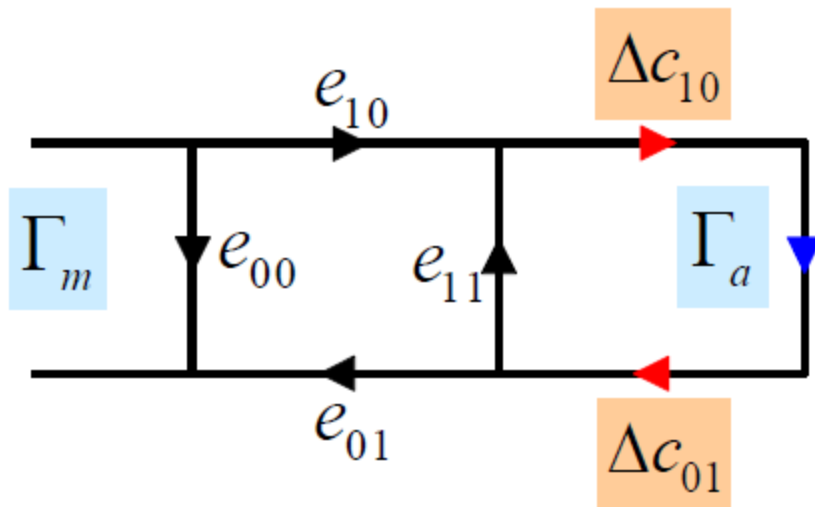
User Defined Debye Cole

Cole Cole-Davidson

Permittivity Data

# Refresh calibration

If the perturbation is small, the change can be characterized by the measuring of a single calibration standard.



$\Gamma_m$  = Measured  $S_{11}$

$\Gamma_a$  = Actual  $S_{11}$

$e_{00}$  = Directivity error

$e_{11}$  = Source match error

$e_{10}$   $e_{01}$  = Reflection tracking error

$\Delta c_{10}$   $\Delta c_{01}$  = Perturbation term



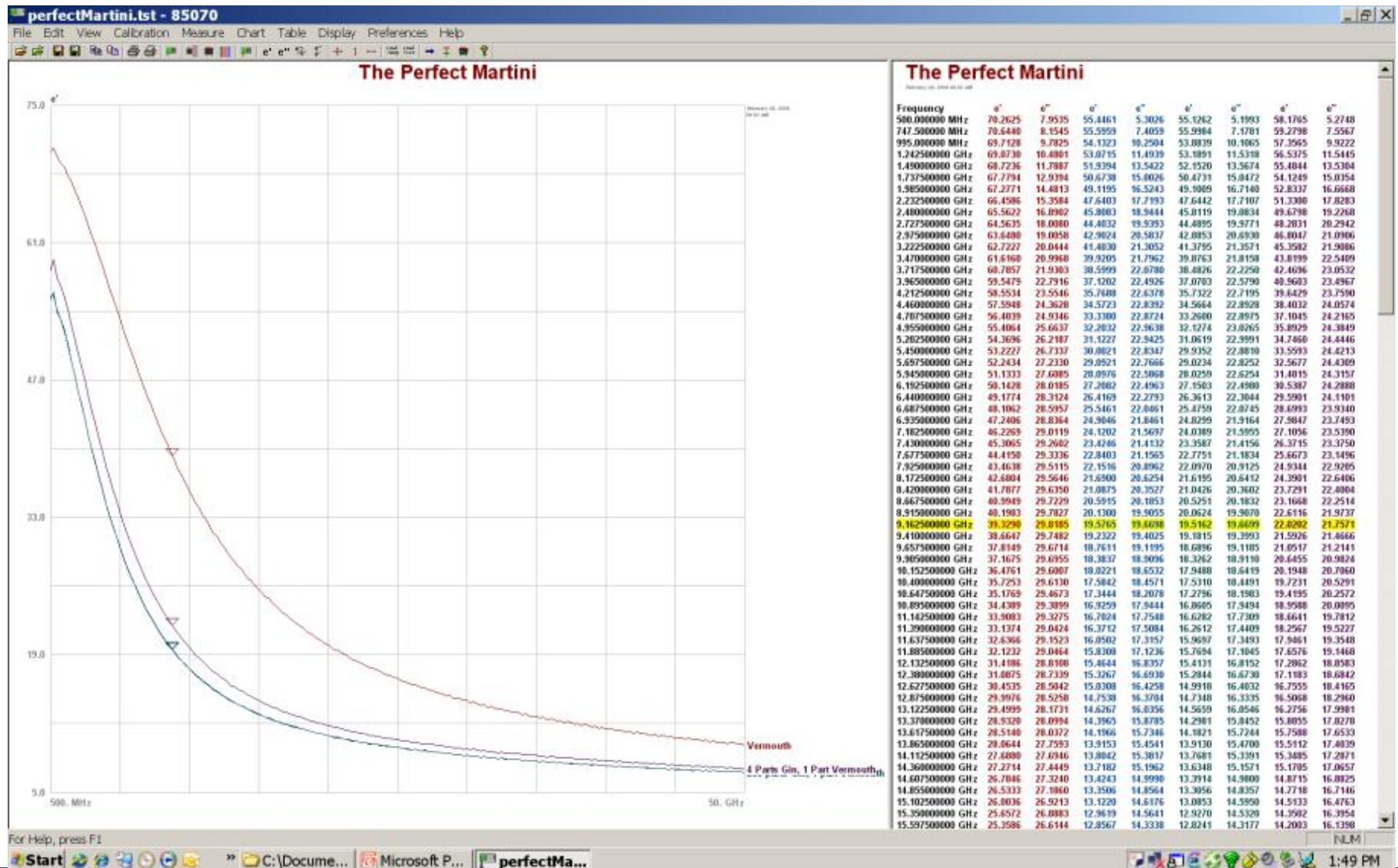
# Coaxial probe example data

## The perfect martini

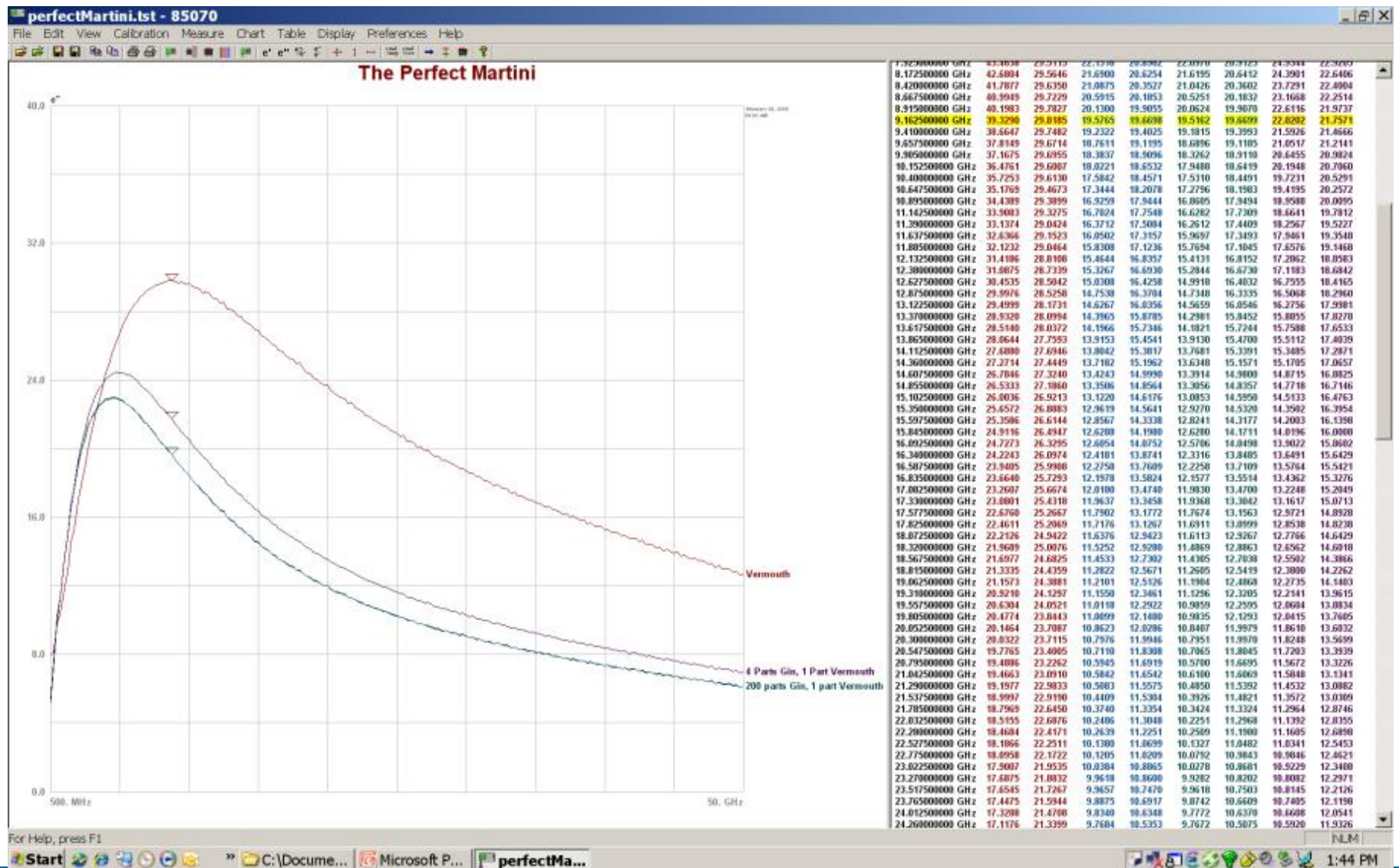




# Coaxial probe example data



# Coaxial probe example data

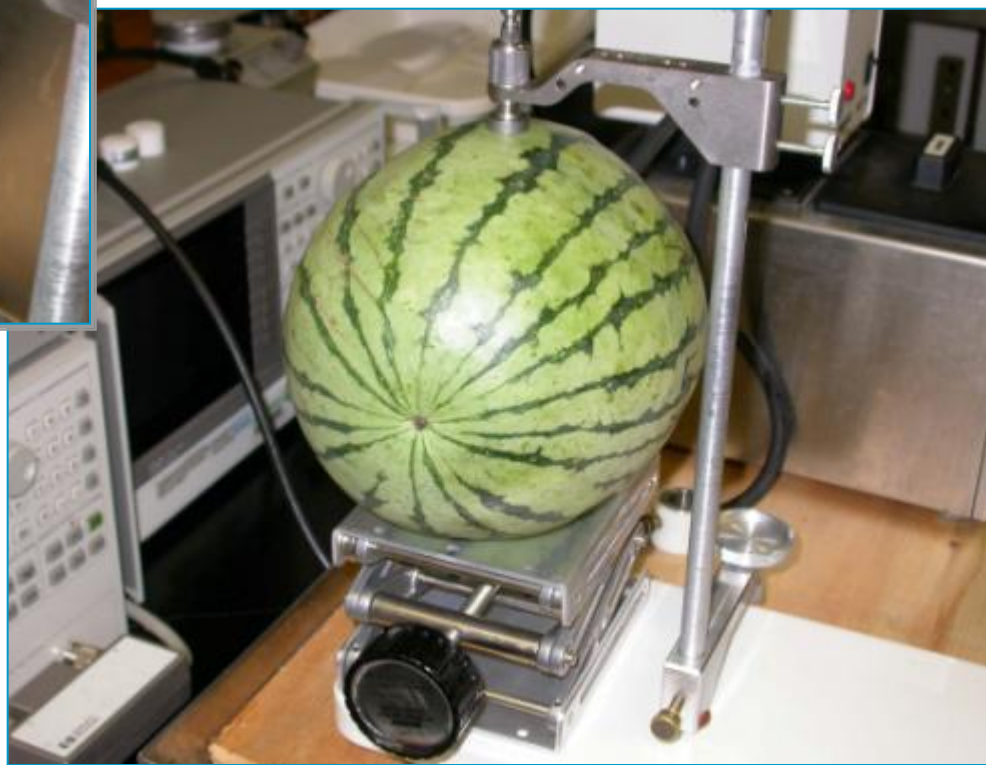




# USDA Fruit ripeness research



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# CPAC Carbon nanotube research



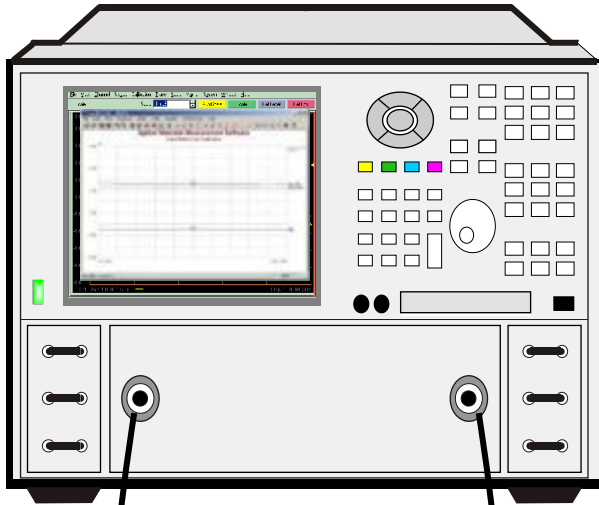
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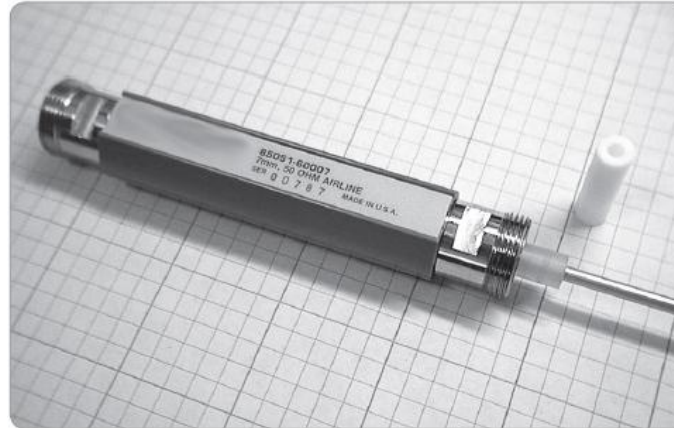
# Transmission line system

Network Analyzer

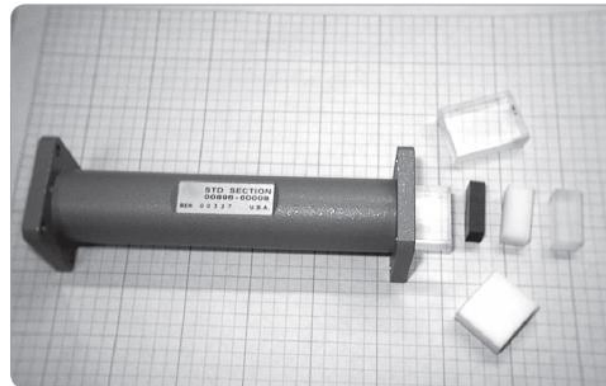
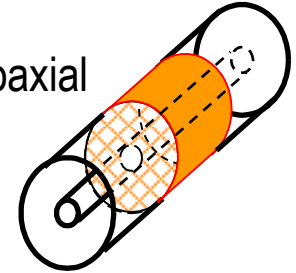


Sample holder  
connected between coax cables

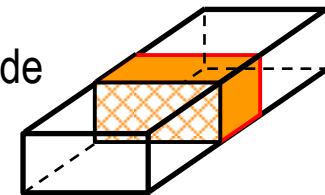
Calibration is required



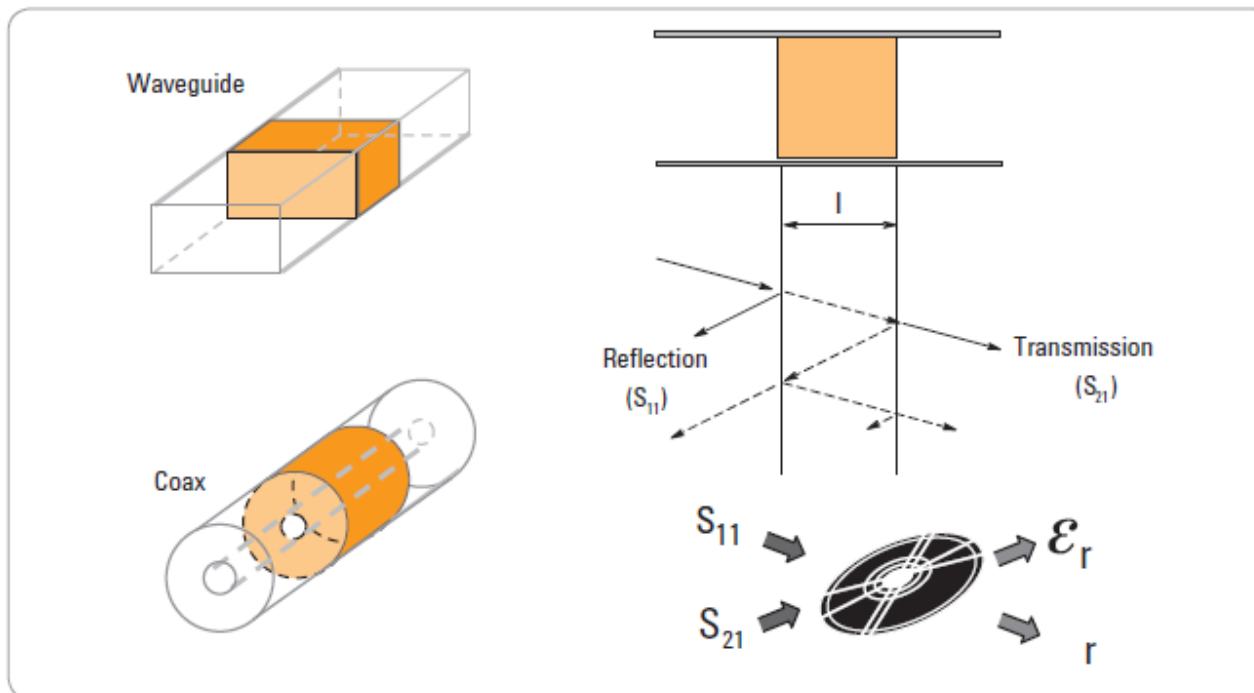
Coaxial



Waveguide



# Transmission line



## Technique features:

- Broadband (low freq. limited by practical sample length)
- Limited low loss resolution (depends on sample length)
- Measures magnetic materials
- Anisotropic materials can be measured in waveguide

## Assumptions:

- Sample fill fixture across section
- No air gaps at fixture walls
- Smooth, flat faces, perpendicular to long axis
- Homogeneous

# Transmission algorithms

Algorithm	Measured S-parameters	Output
Nicolson-Ross	S11,S21,S12,S22	$\epsilon_r$ and $\mu_r$
Precision (NIST)	S11,S21,S12,S22	$\epsilon_r$
Fast	S21,S12	$\epsilon_r$

(85071E also has three reflection algorithms)



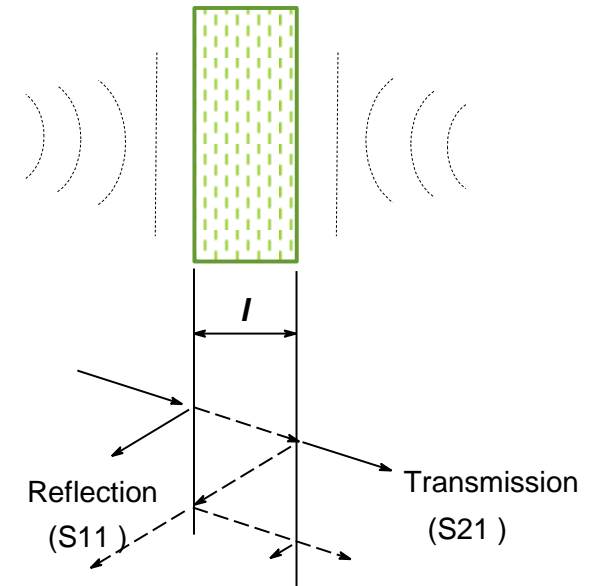
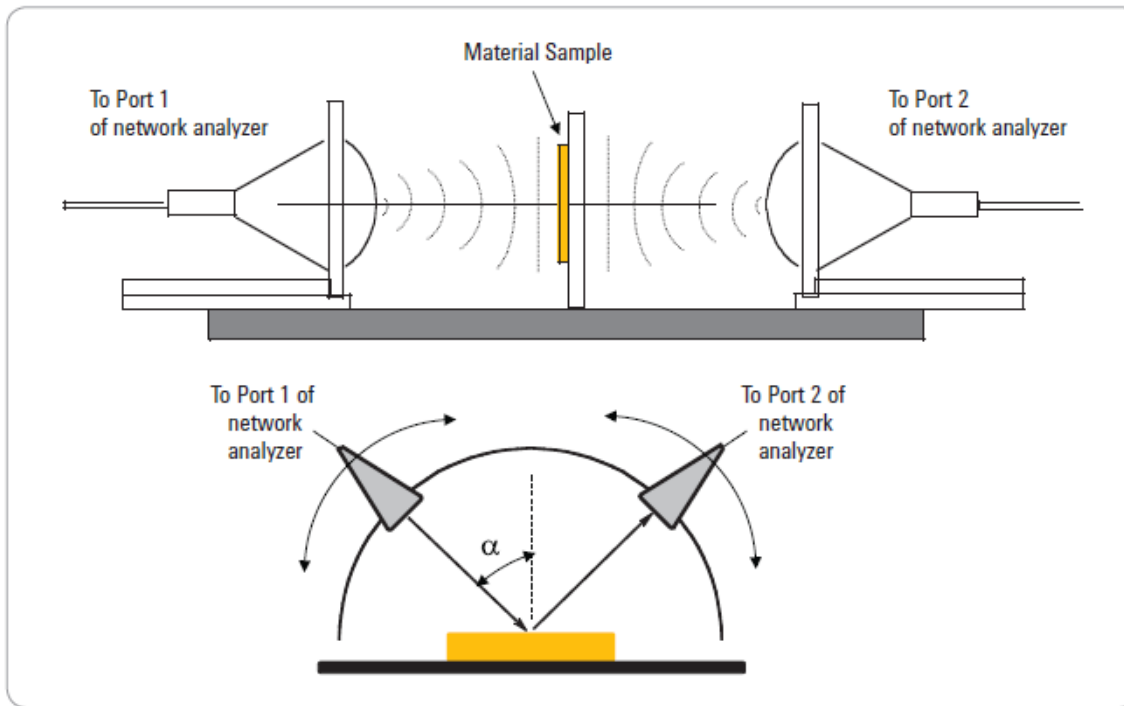
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# Free space system



Dielectric measurement setup for free space measurement

# Free space system



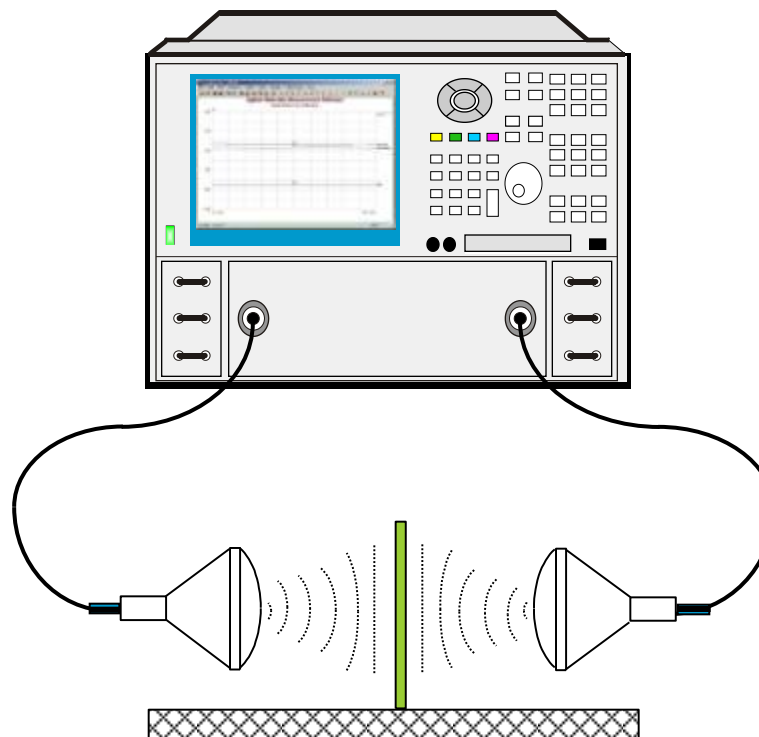
## Technique features:

- Non-contacting, non-destructive
- High frequency (low freq. Limited by practical sample size)
- Useful for high temperature
- Antenna polarization may be varied for anisotropic materials
- Measures magnetic materials

## Assumptions:

- Flat parallel faced samples
- Sample in non-reactive region
- Beam spot is contained in sample
- Known thickness  $> 20/360 \lambda$

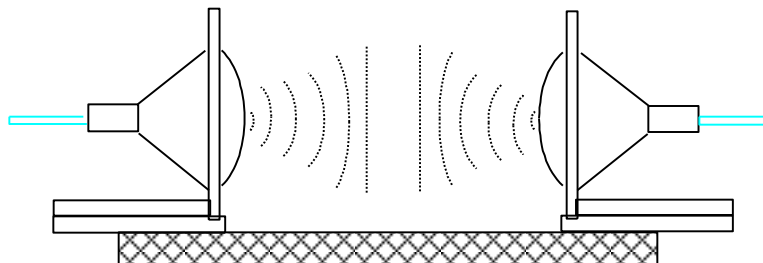
# Free space system requires calibration



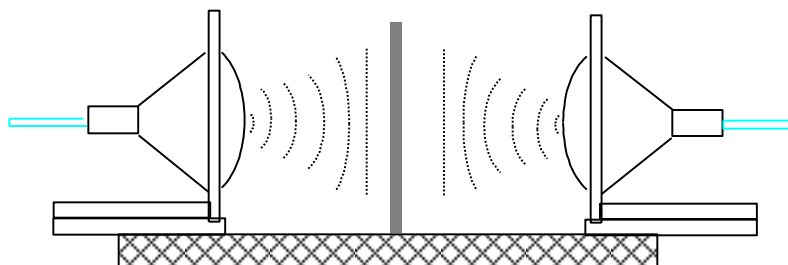
Before a measurement can be made, a calibration must be performed to remove systematic errors.

# TRL calibration

Thru

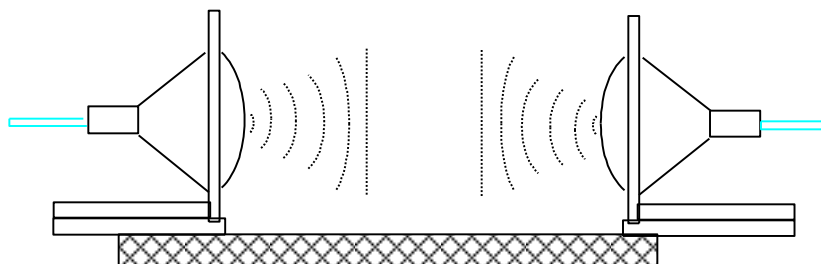


Reflect



Move the antenna away to compensate for the thickness of the short. Move it back for the next step.

Line

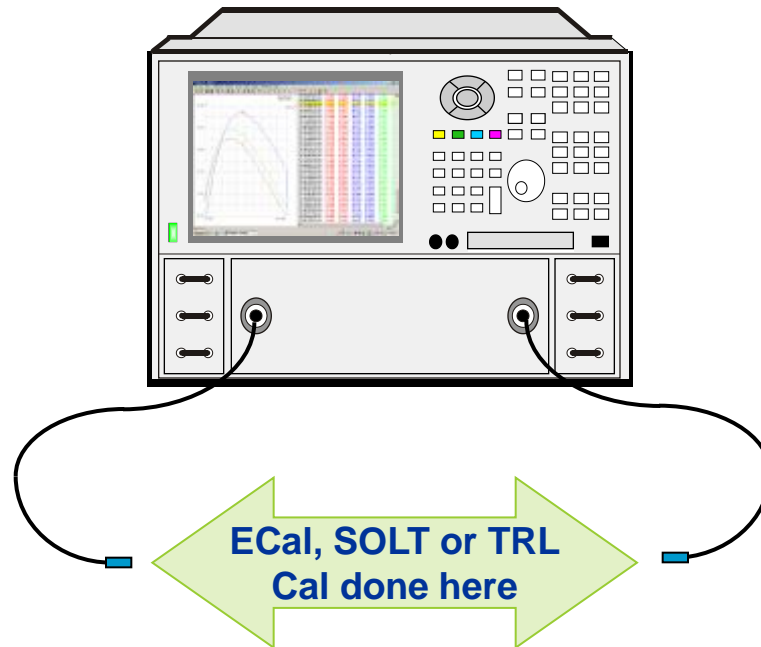


Move the antenna away on a quarter-wavelength and then back in the original position.

## Two Tiered Calibration

1.

Two port calibration at waveguide or coax input into antennas removes errors associated with network analyzer and cables.

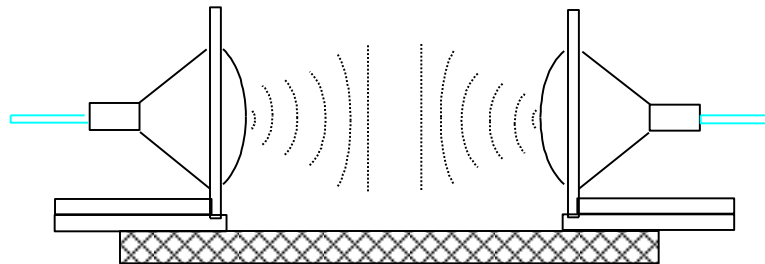


## Two Tiered Calibration

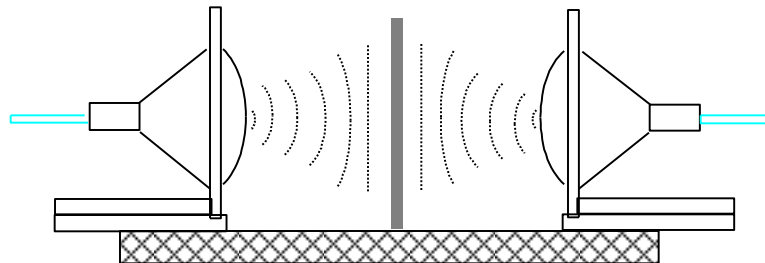
**2.**

Two additional free space calibration standards remove errors from antennas and fixture.

**Line**  
(empty fixture)

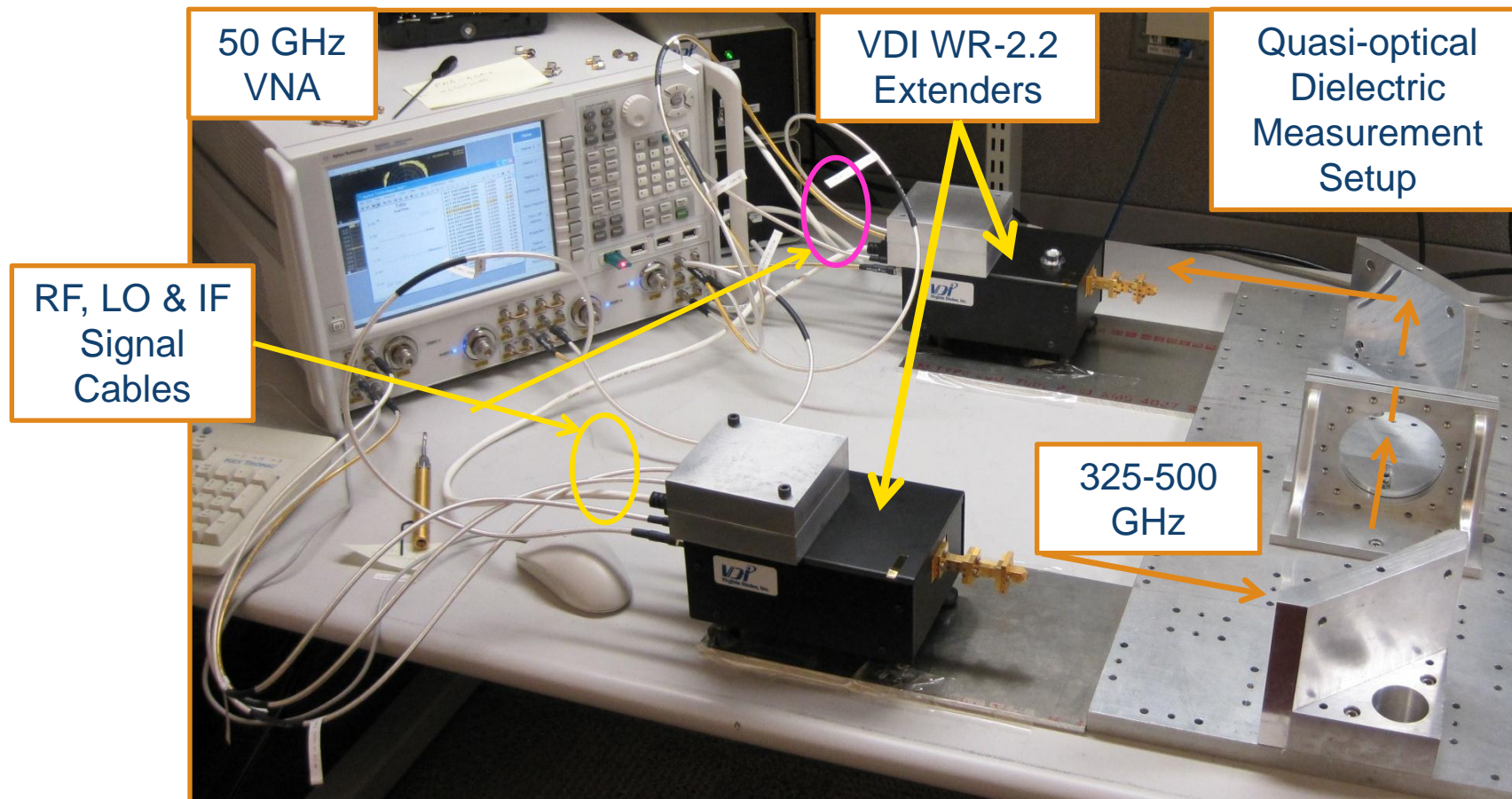


**Reflect**  
(metal plate of known thickness)





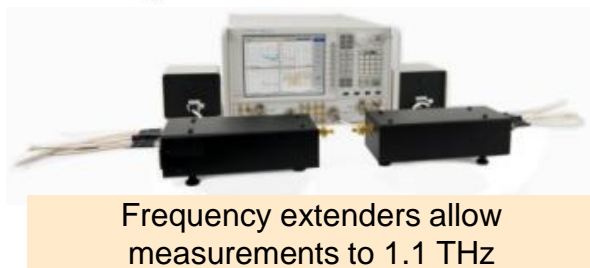
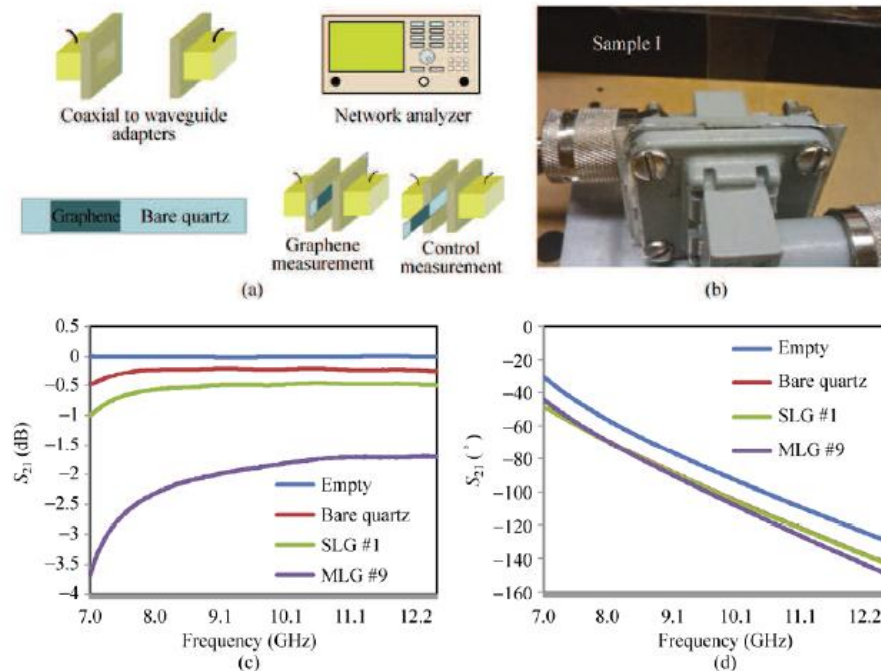
# Quasi-optical VNA measurements



- Quasi-optical dielectric measurements performed at Agilent

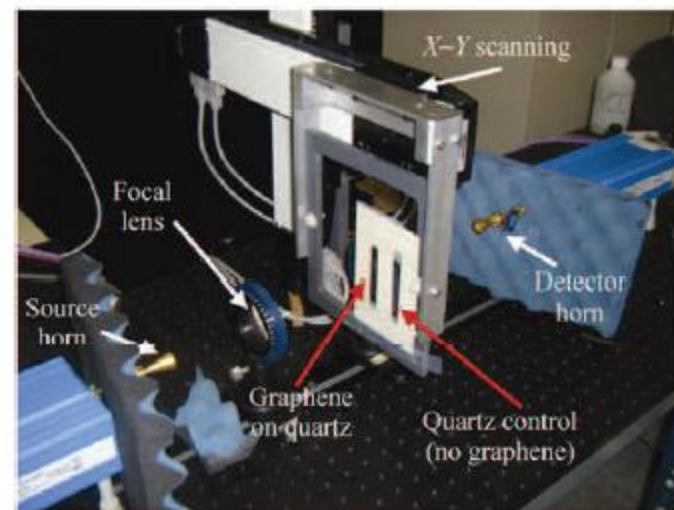


# THz graphene characterization



## Measurement details

Frequency domain measurements of the absolute value of multilayer graphene (MLG) and single-layer graphene (SLG) sheet conductivity and transparency from DC to 1 THz



**Figure 7** Picture of X-band imaging and quasi-optic transmission apparatus

## Paper details

### Terahertz Graphene Optics

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- Introduction
- Permittivity and permeability
- Measurement techniques and systems
- Parallel plate
- Coaxial probe
- Transmission line
- Free space
- **Resonant cavity**

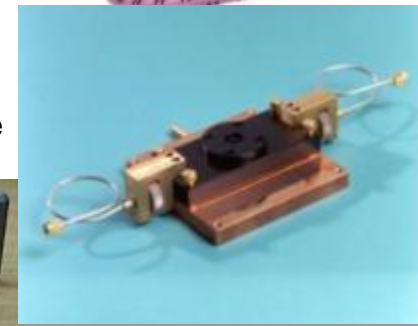
# Resonant cavity system



Agilent Split Cylinder Resonator  
IPC TM-650-2.5.5.5.13



ASTM 2520 Waveguide  
Resonators



Split Post Dielectric  
Resonators from QWED

# Resonant cavity technique

$f_c$  = Resonant Frequency of Empty Cavity

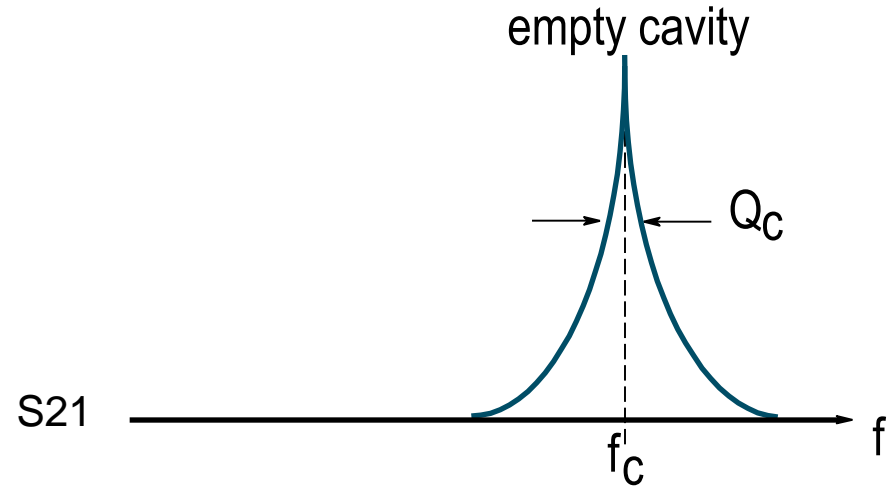
$f_s$  = Resonant Frequency of Filled Cavity

$Q_c$  = Q of Empty Cavity

$Q_s$  = Q of Filled Cavity

$V_s$  = Volume of Empty Cavity

$V_c$  = Volume of Sample



$$\epsilon'_r = 1 + \frac{V_c(f_c - f_s)}{2V_s f_s} =$$
$$\epsilon''_r = \frac{V_c}{4V_s} \left( \frac{1}{Q_s} - \frac{1}{Q_c} \right)$$

ASTM 2520

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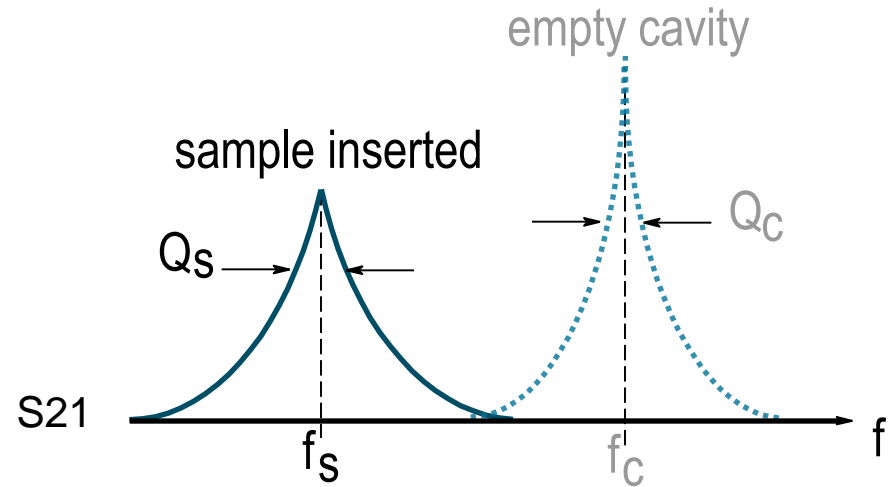
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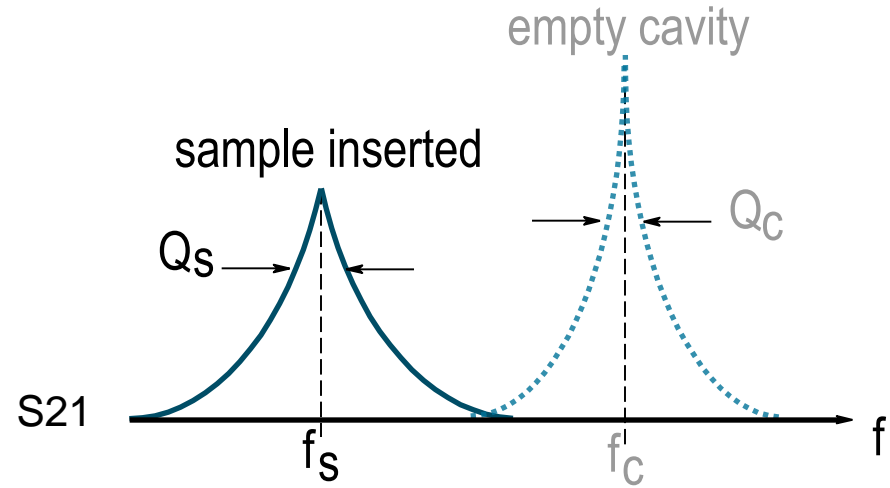
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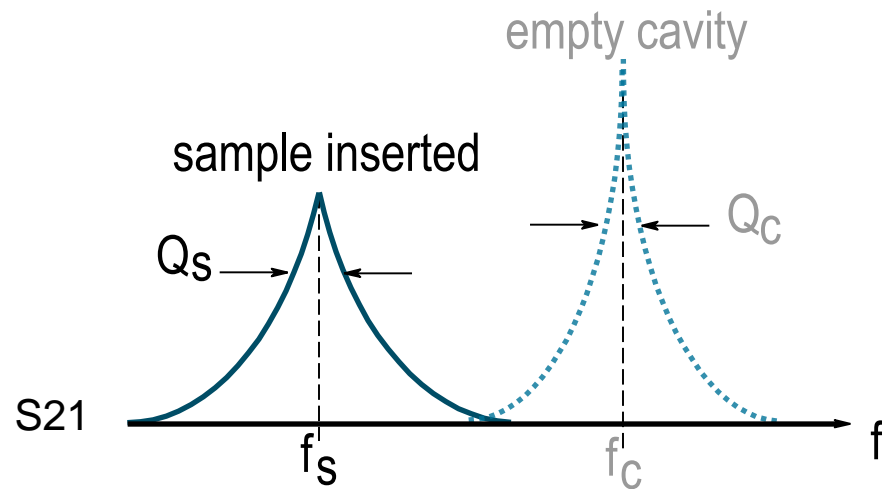
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# Resonant cavity example data

85071E option 300

Measurement Method: Split Cylinder

Measurement Instrument: PNA Series

Instrument Interface: DCOM

GPIB Address:   
 NWA Address:

Save Setup Recall Setup

Save Data Copy Data

About Exit

Measurement

Cavity  $F_s$  = 10.0362596 GHz  
Cavity Q = 21868.3 Measure

Sample thickness: 1.52 mm Set Range

Sample  $F_s$  = 9.66124915 GHz  
Sample Q = 12962.7 Measure

Calculated  $\epsilon_r'$  = 2.05318  
Calculated  $\epsilon_r''$  = 0.00046  
Loss tangent = 0.00022 Recalculate

Measurement Wizard

Cont. CH 1: S21 No Cor LCL



# Resonant vs. broadband transmission



Unlocking Measurement Insights for 75 Years

	Resonant	Broadband
Low Loss materials	Yes $\epsilon_r''$ resolution $\leq 10^{-4}$	No $\epsilon_r''$ resolution $\geq 10^{-2}$ - $10^{-3}$
Thin Films and Sheets	Yes 10GHz sample thickness <1mm	No 10GHz optimum thickness ~ 5-10mm
Calibration Required	No	Yes
Measurement Frequency Coverage	Discrete Frequencies	Broadband or Banded

# Summary technique and strengths

Coaxial Probe

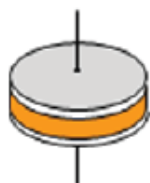
$\epsilon_r$



Broadband, convenient, non-destructive  
Best for lossy MUTs; liquids and semi-solids

Parallel Plate

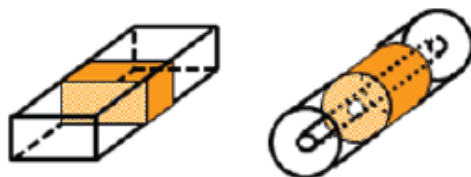
$\epsilon_r$



Accurate  
Best for low frequencies; thin, flat sheets

Transmission Line

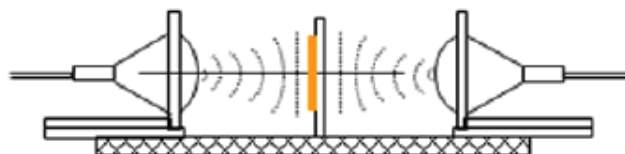
$\epsilon_r$  and  $\mu_r$



Broadband  
Best for lossy to low loss MUTs;  
machineable solids

Free Space

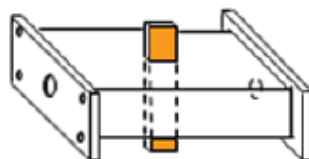
$\epsilon_r$  and  $\mu_r$



Broadband; Non-contacting  
Best for flats sheets, powders, high temperatures

Resonant Cavity

$\epsilon_r$



Single frequency; Accurate  
Best for low loss MUTs; small samples

R N Clarke (Ed.), *“A Guide to the Characterisation of Dielectric Materials at RF and Microwave Frequencies,”* Published by The Institute of Measurement & Control (UK) & NPL, 2003

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# Thank you!



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